

# Maths Module 1: Numbers

## Student's Book

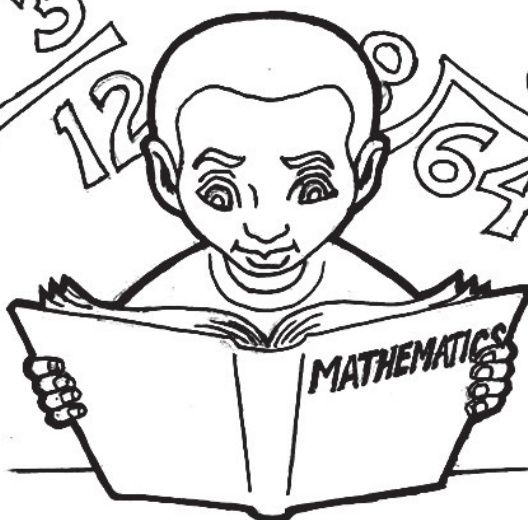
%

0.334

$$\begin{array}{r} 2591 \\ + 2107 \\ \hline 4698 \end{array}$$

1, 3, 5, 7...

$$\begin{array}{r} 4 \times 3 \\ \hline 12 \end{array} \quad \begin{array}{r} 9 \\ 64 \overline{) 8} \end{array}$$



6 9 2  
2 2

$\pi$

# Maths Module 1: Numbers

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# 1. Whole Numbers

## 1.1 Introduction

A **whole number** is a number with no fraction or decimal part, 100, 250 and 1000 are whole numbers.

### Think

When do we use whole numbers in our everyday life? Think of some examples.

*Dave is very bad at Maths. One day he went to the market and spent 23 baht on vegetables. He paid with a 100 baht note. The shopkeeper gave him 57 baht change. Dave took the money and went home.*

He made a mistake. What was it?

He would not have made this mistake if he was good at maths.

## 1.2 Place Value

The position of a number tells us its **value**.

ten thousands	thousands	hundreds	tens	units
4	7	2	8	6

### Think

What is the value of the 8 in this number?

What about the 4?

Write the number in words.

### Practice

i. Write these numbers in words

a) 204

b) 1023

c) 9552

d) 10,256

e) 81,505

f) 370,000

ii. Write these numbers in figures

a) seven hundred and five

b) two thousand six hundred and fifty two

c) twenty two thousand five hundred

d) one million two hundred and fifty seven thousand

iii. Make as many different numbers as you can from the figures 2, 6, 7, 0, 3. Arrange the numbers in **order**, starting with the smallest.

## 1.3 Rounding

We don't always need to know a number exactly. Sometimes we use **rounding** to give an **estimate**.

**Example** - The population of Mae La is 48,492.

To round to the nearest *hundred* we look at the number in the *tens* column.

It is greater than 5 so we round up. To the nearest hundred the population of Mae La is 48,500.

0 1 2 3 4 | 5 6 7 8 9



If the number is **less than 5**, we **round down**.



If the number is **greater than or equal to 5**, we **round up**.

### Practice

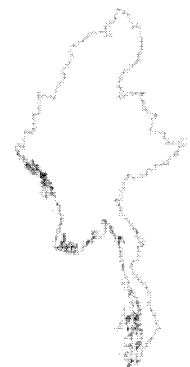
a) What is the population of Mae La to the nearest thousand. Did you round up or down? Why?

b) The exact number of tickets sold for an Ironcross concert in Rangoon was 9782. How many tickets were sold to the nearest hundred?



c) Yesterday the Rangoon Times newspaper sold 56,792 copies. How many copies were sold to the nearest thousand?

d) The population of Burma is 47,382,683. To the nearest million how many people live in Burma?



We can also use rounding to check our calculations.

**Example** - Use rounding to check that the answer to the sum is correct.

$$\begin{array}{r} 2389 \\ + 1467 \\ \hline 3856 \end{array}$$

2389 to the nearest hundred is 2400, 1467 to the nearest hundred is 1500.  $2400 + 1500 = 3900$ .

This estimate is close to our answer, so it is probably correct.

If the answer and the estimate are very different, then we know something is wrong!

## 1.4 Addition and Subtraction

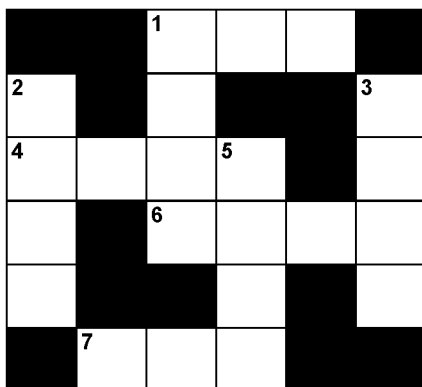
One important **property** of **addition** is that we can add numbers in any order and the answer will be the same.  $5 + 3 + 8 = 8 + 5 + 3$ . This property is called the **commutative law** of addition.

The commutative law is not true for **subtraction**.  $5 - 3 - 8 \neq 8 - 5 - 3$ .

**Addition is commutative. Subtraction is not commutative.**

### Practice

i. Solve the crossword using the clues.  
Use rounding to check your answers.



#### Across

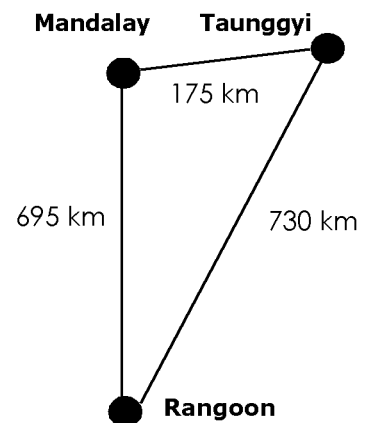
1. Add:  $165 + 256$   
4. Add:  $943 + 468$   
6. Add:  $1159 + 4457$   
7. Add:  $439 + 320$

#### Down

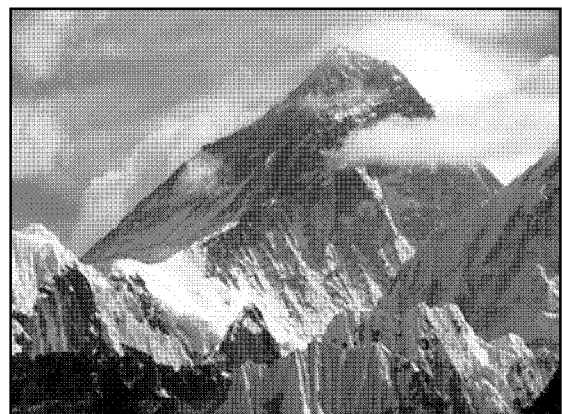
1. Subtract:  $5270 - 655$   
2. Subtract:  $2563 - 417$   
3. Subtract:  $2748 - 1584$   
5. Subtract:  $2252 - 553$

ii. Min Too has to go from Rangoon to Taunggyi and then to Mandalay. How far is his journey?

He goes back to Rangoon directly. How much shorter is his journey home?



iii. Ben Nevis is the highest mountain in Britain. It is 1343 m high. Mount Everest is the highest mountain in the world. It is 8843 m high. How much higher is Mount Everest than Ben Nevis?



Camp population figures - June 2006			
	Female	Male	Total
<b>Chiang Mai Province</b>			
Wieng Haeng	314	286	
<b>Mae Hong Son Province</b>			
Ban Mai Nai Soi	9204	9878	19082
Ban Mae Surin	1740	1894	3634
Mae La Oon	7613	8307	
Mae Ra Ma Luang	7384	7650	15034
Total populations for Mae Hong Song	25941	27729	53670
<b>Tak Province</b>			
Mae La	23732	24760	48492
Umpiem Mai	9439	10172	19611
Nu Po	6529	6936	13465
Total populations for Tak		41868	81568
<b>Kanchanaburi Province</b>			
Ban Don Yang	2251	2198	4449
<b>Ratchaburi Province</b>			
Tham Hin	5198	5373	10571
Total populations for Thailand		77454	150858

iv. The table shows the number of people who live in each of the refugee camps on the Thai-Burma border. Answer the questions to complete the table. Before you fill in the gaps use rounding to check your answer.

- What is the total population of Wieng Haeng camp?
- What about the population of Mae La Oon camp?
- What is the total number of females in the camps in Tak province?
- Use your answer for c) to calculate the total number of female refugees in all the camps. How else could you calculate this figure?

## 1.5 Multiplication and Division

### Think

Solve each calculation. Now write the numbers in a different order and solve again. What do you notice?

a)  $2 \times 4 \times 6 =$

c)  $6 \times 9 \times 8 =$

b)  $10 \div 2 \div 5 =$

d)  $32 \div 4 \div 2 =$

The exercise shows us that **Multiplication** is commutative. The order you calculate is not important. **Division** is not commutative. The order we calculate is important.

The commutative law can make calculations easier:

**Example - Calculate  $10 \times 3 \times 22$ .**

$$10 \times 3 \times 22 = 22 \times 3 \times 10 = 66 \times 10 = 660$$

### Think

When we multiply by 10 we add a zero to the number. What about when we multiply by 100? 1000?

Here are two more methods to make multiplication easier:

**Example - Splitting method.**

Calculate  $17 \times 6$ . We know  $6 = 2 \times 3$ .

$$17 \times 6 = 17 \times 2 \times 3 = 34 \times 3 = 112$$

**Example - Rounding method. Calculate  $49 \times 6$ .**

First, we round 49 to 50.

$$49 \times 6 = 50 \times 6 - 1 \times 6 = 300 - 6 = 294$$

## Practice

i. Choose a method for each question and calculate:

- |                            |                            |
|----------------------------|----------------------------|
| a) $47 \times 7$           | e) $10 \times 35 \times 2$ |
| b) $10 \times 5 \times 11$ | f) $67 \times 8$           |
| c) $13 \times 9$           | g) $8 \times 21$           |
| d) $21 \times 8$           |                            |

ii. Solve the following:

- a) A school day is 7 hours.  
How many minutes is this?
- b) A litre of petrol costs 28 baht.  
How much do 12 litres cost?
- c) Mama noodles cost 6 baht a packet.  
How much do 52 packets cost?

For larger numbers we use **long multiplication**

### Example - Find $84 \times 26$

$84 \times 26 = 84 \times 6 + 84 \times 20$ . So,

$$\begin{array}{r} 84 \\ \times 26 \\ \hline 504 \quad (84 \times 6) \\ + 1680 \quad (84 \times 20) \\ \hline 2184 \quad (504 + 1680) \end{array}$$

## Practice

Use long multiplication to calculate

- |                    |                     |
|--------------------|---------------------|
| a) $355 \times 25$ | d) $241 \times 32$  |
| b) $462 \times 33$ | e) $1251 \times 28$ |
| c) $589 \times 62$ | f) $146 \times 259$ |

## Activity

Multiply the number 123456789 by 3, then multiply the result by 9.

Now multiply 123456789 by 5 and then again by 9. What do you notice?

What will the answer be if you multiply by 4 then 9? What about multiplying by 7 and then 9?

## 1.6 Order of Operations

In maths an **operation** is something we do to a number. Multiplication, division, addition and subtraction are all operations. If we have a calculation with more than one operation, the order we operate is important.

## Think

- a) Look at these calculations.  
What order should we do the operations?

$$\begin{array}{l} 6 + 4 \times 7 - 13 \\ 37 - 35 \div 5 \\ 8 \times 4 + 15 \div 3 \end{array}$$

We can use similar methods for division as we do for multiplication.

## Think

Which multiplication method can be used to calculate  $816 \div 6$ ? What is the answer?

## Practice

Use the splitting method to calculate

- |                 |                  |
|-----------------|------------------|
| a) $56 \div 4$  | c) $112 \div 16$ |
| b) $90 \div 15$ | d) $720 \div 24$ |

**Example - Use long division to calculate  $21 \overline{)2678}$ .**

$$\begin{array}{r} 21 \overline{)2678} \\ 21 \overline{)26} \quad \text{There is 1 twenty-one in 26, remainder 5.} \\ \underline{21} \quad \text{There are 2 twenty-ones in 57, r 15.} \\ 57 \quad \text{There are 7 twenty-ones in 26, r 11.} \\ \underline{42} \quad \text{There are 7 twenty-ones in 26, r 11.} \\ 158 \\ \underline{147} \\ 11 \end{array}$$

$21 \overline{)2678} = 127 \text{ r } 11$

## Practice

Use Long division to calculate:

- |                          |                          |
|--------------------------|--------------------------|
| a) $48 \overline{)576}$  | d) $38 \overline{)9728}$ |
| b) $35 \overline{)8050}$ | e) $33 \overline{)8392}$ |
| c) $18 \overline{)4824}$ | f) $27 \overline{)6732}$ |

## Practice

Complete the calculations:

- a)  $5 \times 4 + 2 \times 3$
- b)  $16 + 3 \times 4 - 2$
- c)  $9 - 8 + 5 \times 2$
- d)  $8 + 4 \times 0$
- e)  $5 \times 4 \div 10 + 6$
- f)  $19 + 3 \times 2 - 8 \div 2$
- g)  $4 \times 2 - 6 \div 3 + 3 \times 2 \times 4$

If a calculation contains **brackets** then what is inside the brackets must be calculated *first*.

**Example - Calculate  $2 \times (3 + 5)$**

$$2 \times (3 + 5) = 2 \times 8 = 16$$

$3^2$  is read as **three squared** or **to the power of 2**.

$$3^2 = 3 \times 3 = 9.$$

$3^3$  is read as **3 cubed** or **3 to the power of 3**.

$$3^3 = 3 \times 3 \times 3 = 27.$$

If a calculation contains **powers** then we calculate them *after* the brackets.

**Example - Calculate  $(3 + 5)^2 - 8 \times 4$**

$$(3 + 5)^2 - 8 \times 4 = 8^2 - 8 \times 4 = 64 - 32 = 32$$

**Example - Calculate  $4 + \frac{8}{5-3}$**

$$4 + \frac{8}{5-3} = 4 + \frac{8}{2} = 4 + 4 = 8$$

$$\frac{8}{5-3} \text{ means } 8 \div (5-3) = 8 \div 2 = 4$$

## Practice

i. Insert the missing operation to make each statement correct:

- a)  $5 - 4 + 1 = 5 \_ 1 \_ 4$
- b)  $120 \div 6 \times 2 \div 10 = 120 \_ 10 \_ 6 \_ 2$
- c)  $19 + 7 - 12 + 5 = 19 \_ 12 \_ 5 \_ 7$
- d)  $18 \div 3 + 2 \times 6 - 4 = 2 \_ 6 \_ 4 \_ 18 \_ 3$

ii. Put brackets in the statements to make them true:

- a)  $12 \div 3 \times 2 = 2$
- b)  $4 \times 5 + 7 = 48$
- c)  $8 + 6 \div 3 + 2 = 12$
- d)  $27 - 5 \times 9 - 5 = 88$

iii. Calculate the value of:

- a)  $2 \times (7 - 2) \div (16 - 11)$
- b)  $12 - 8 - 3 \times (9 - 8)$
- c)  $(5 + 3) \times 2 + 10 \div (8 - 3)$
- d)  $8^2 + 5^2 + 6^2$
- e)  $28 - (9 - 7)^2$
- f)  $72 \div (5 - 2)^2$
- g)  $(52 - 42)^3$
- h)  $\frac{(2+3)^2}{(14-9)^2}$

iv. Write each calculation using brackets and solve:

a) Three students went to the shop after school. One student bought 3 cakes for 2 baht each. One student bought 3 packets of coffee mix for 3 baht each. The third student bought 3 sweets for 1 baht each. How much money did they spend all together?

b) Two sisters have money boxes. There are five 2 baht coins and four 1 baht coins. The second box has six 2 baht coins and ten 1 baht coins. What is the total amount of money?

c) Mae Sot youth club had 82 members at the beginning of 2006. In March 32 left. In May 27 joined and 12 more left. How many students were in the club at the beginning of June?

Use this diagram to help you remember the **order of operations**:

**brackets** → **powers** → **division and multiplication** → **addition and subtraction**

## Think

Make different answers by putting brackets into the calculation  $3 \times 5 - 2 \times 7 + 1$ .

For example:  $(3 \times 5) - (2 \times 7) + 1 = 2$ .

Write some more examples and give them to your partner. Put brackets into your partner's examples to make different answers.

**Activity** - For this you need ten cards numbered 0 - 9.

Turn the cards over. Take two cards to make a 2-digit number. Take four more cards.

With the four cards, try to make an expression using brackets, operations and powers that is equal to your 2-digit number.

You get points for the difference between your answer and the 2-digit number.

Try to get a low score.

Example. My two digit number is 47. My four numbers are 1, 3, 8, 5.

$(8 \times 5) + 1 + 3 = 44$  scores 3 points because  $47 - 44 = 3$ .

$(1 + 8) \times 5 + 3 = 48$  scores 1 point because  $48 - 47 = 1$ .

Try once. Shuffle the cards and take some new numbers.

Play 10 times. The person with the lowest score wins.

## 2. Factors and Multiples

### 2.1 Introduction

When 12 is divided by 3, the remainder is zero.

We say that 3 is a **factor** of 12.

#### Think

What are the other factors of 12? What are the factors of 18?

We can write a number as the **product** of two factors:  $1 \times 12$ ,  $3 \times 4$ ,  $2 \times 6$  are all equal to 12.

#### Practice

Write each number as a product of two factors:

a) 18

b) 24

c) 27

d) 36

e) 64

f) 80

g) 96

h) 144

12 divided by 2 is equal to a whole number. We say that 12 is a **multiple** of 2.

12 is also a multiple of 1, 3, 4, 6 and 12.

#### Practice

i. Complete the sentences:

a) 15 is a multiple of \_\_, \_\_, \_\_ and 15

b) 27 is a multiple of 1, \_\_, \_\_ and \_\_

c) 40 is a multiple of \_\_, 4, \_\_, \_\_, \_\_, \_\_

d) 41 is a multiple of \_\_ and \_\_

ii. Answer the following:

a) Write down all the multiples of 3 between 20 and 40.

b) Write down all the multiples of 7 between 25 and 60.

c) Write down all the multiples of 13 between 25 and 70.

### 2.2 Prime Numbers

Some numbers only have two factors. The factors of 3 are 1 and 3. The factors of 5 are 1 and 5.

3 and 5 are called **prime numbers**. 1 is not a prime number because it only has one factor.

#### Think

Is this statement true or false?

Explain your answer:

'The only even prime number is 2'

#### Practice

Answer the following:

a) Which numbers are prime numbers?:  
2, 3, 4, 5, 6, 7, 8, 9, 10, 11, 12

b) Write down all the prime numbers between 21 and 30.

c) Write down all the prime numbers between 30 and 50.

**Activity** - Look at the numbers below. 1 is crossed out. 2 is circled.

Write the numbers 1-100 in your book.

Cross out all the multiples of 2.

Circle 3 and cross out all the multiples of 3.

Circle 5 and cross out all the multiples of 5.

Circle 7 and cross out all the multiples of 7.

Continue until all numbers are circled or crossed out.

Write out all the numbers that are not circled or crossed out. What are these numbers?

1    ②    3    4    5



## 2.3 Indices

We learnt in Section 1.5 that  $3^3$  is read as '3 cubed' or '3 to the power of 3'.  $3^3 = 3 \times 3 \times 3 = 27$ . The power is called the **index**. (The plural of index is **indices**).  $3^3$  is  $3 \times 3 \times 3$  written in **index form**.

### Practice

i. Write the numbers in index form:

- a)  $3 \times 3$
- b)  $2 \times 2 \times 2$
- c)  $5 \times 5 \times 5 \times 5$
- d)  $7 \times 7 \times 7 \times 7 \times 7$
- e)  $13 \times 13 \times 13 \times 13$
- f)  $2 \times 2 \times 3 \times 3$
- g)  $3 \times 3 \times 3 \times 5 \times 5$
- h)  $3 \times 11 \times 11 \times 2 \times 2$
- i)  $13 \times 5 \times 13 \times 5 \times 13$

ii. Find the value of:

- a)  $3^3$
- b)  $2^5$
- c)  $5^2$
- d)  $3^4$
- e)  $7^2$
- f)  $2^3 \times 3$
- g)  $2^3 \times 3^2$
- h)  $3^2 \times 5^2$
- i)  $2 \times 3^3 \times 7$

Remember that multiplication is commutative!

## 2.4 Prime Factors

A **prime factor** is a prime number that is a factor of another number. 3 is a prime number and a factor of 9 so it is a prime factor of 9.

These rules can help us find prime factors:

- A number is divisible by 2 if the last digit is even.
- 3 if the sum of the digits is divisible by 3.
- 5 if the last digit is 0 or 5.

### Practice

Are these numbers divisible by 2, 3 or 5?:

- a) 525
- b) 747
- c) 740
- d) 1424

Any whole number that is greater than 1 can be written as a product of prime factors.

**Example** - Write 720 as a product of prime factors.

**Method 1:** Start by dividing by 2.

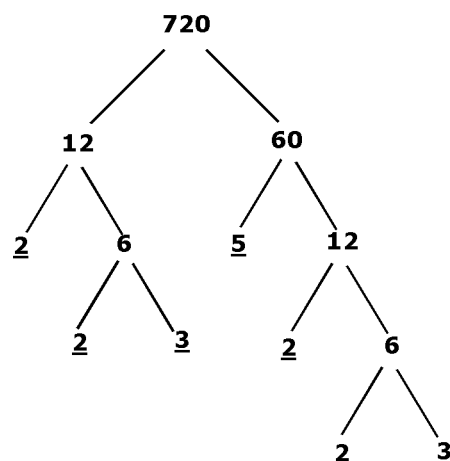
2	720
2	360
2	180
2	90
3	45
3	15
5	5
	1

45 is not divisible by 2.  
We try to divide by 3.

5 is not divisible by 3.  
We divide by 5.

$$\begin{aligned} \text{We have } 720 &= 2 \times 2 \times 2 \times 2 \times 3 \times 3 \times 5 \\ &= 2^4 \times 3^2 \times 5 \end{aligned}$$

**Method 2:** Use a factor tree.



The underlined numbers are the prime factors.

$$\begin{aligned} \text{We have } 720 &= 2 \times 2 \times 3 \times 5 \times 2 \times 2 \times 3 \\ &= 2 \times 2 \times 2 \times 2 \times 3 \times 3 \times 5 \\ &= 2^4 \times 3^2 \times 5 \end{aligned}$$

## Think

To use the factor tree we divided 720 into 2 non-prime factors, 12 and 60.  
Find 2 different non-prime factors of 720. Use them in a factor tree to find the prime factors of 720.

## 2.5 Highest Common Factor (H.C.F.)

The **Highest Common Factor (H.C.F.)** of two or more numbers is the biggest number that is a factor of both numbers.

**Example** - Find the H.C.F of 16 and 24.

The factors of 16 are 1, 2, 4, 8 and 16.

The factors of 24 are 1, 2, 4, 6, 8, 12 and 24.

1, 2, 4 and 8 are factors of 16 *and* 24. 8 is the biggest factor. 8 is the Highest Common Factor.

## 2.6 Lowest Common Multiple (L.C.M.)

The **Lowest Common Multiple (L.C.M.)** of two numbers is the smallest number that is a multiple of both numbers.

**Example** - Find the L.C.M. of 6 and 8.

The multiples of 6 are: 6 12 18 **24** 30 36  
42 **48** 54 60 66 **72**.....

The multiples of 8 are: 8 16 **24** 32 40 **48**  
56 64 **72** 80 88 96.....

We can see that common multiples of 6 and 8 are: 24, 48 and 72. 24 is the smallest multiple. 24 is the Lowest Common Multiple.

## Practice

Find the Highest Common Factor of:

- |           |               |
|-----------|---------------|
| a) 9, 12  | d) 30, 45, 90 |
| b) 12, 24 | e) 39, 13, 26 |
| c) 14, 42 | f) 36, 44, 52 |

## Practice

Find the Lowest Common Multiple of:

- |          |               |
|----------|---------------|
| a) 3, 5  | d) 12, 16     |
| b) 6, 8  | e) 4, 5, 6    |
| c) 5, 15 | f) 18, 24, 36 |

**Activity** - For this you need twenty folded pieces of paper numbered 1-20.

Your teacher will divide the class into groups of 4 and then into two teams of two people.

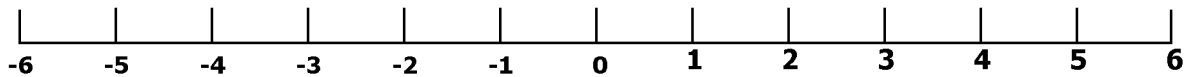
The first team picks two numbers. The second pair has to find the lowest common multiple of the two numbers. If they are right, they get one point. Fold the numbers and put them back.

Now the second pair picks two numbers and the first pair has to find the lowest common multiple. The first team to score 10 points is the winner.

# 3. Negative Numbers

## 3.1 Introduction

Look at the number line. Numbers to the right of zero are **positive numbers**. They are *greater than* zero. The numbers to the left of zero are **negative numbers**. They are *less than* zero.



The positive number 5 means +5, but we don't write the '+' sign. When we write negative numbers, we put a '-' sign in front of the number.

### Think

We know that  $5 > 3$  (5 is greater than 3) and that  $2 < 4$  (2 is less than 4). What about negative numbers? Put the correct sign between the numbers below.

a) -2    -4  
e) 5    1    -3

b) -3    -1  
f) -3    -9    -12

c) -4    1

d) -4    -2    0

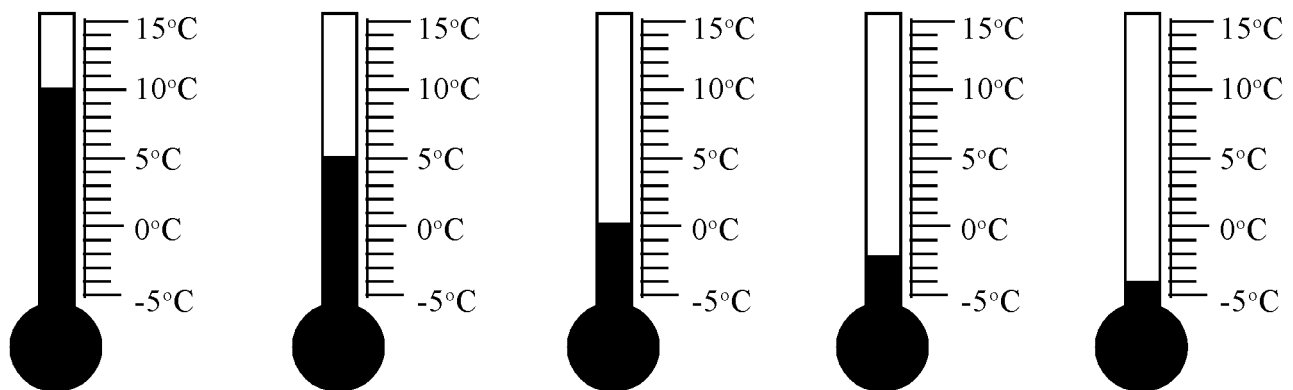
We see that as a negative number increases, its value decreases.

## 3.2 Temperatures

Temperature is measured in degrees Celsius or degrees centigrade. Eight degrees Celsius is written as  $8^{\circ}\text{C}$ . In Science you learn that water freezes at  $0^{\circ}\text{C}$ . The temperature where you live is always greater than  $0^{\circ}\text{C}$ . In England, America and many other countries the temperature is sometimes less than  $0^{\circ}\text{C}$ . Temperatures less than  $0^{\circ}\text{C}$  are written as negative numbers, such as  $-5^{\circ}\text{C}$ . Temperatures are measured using thermometers.

### Practice

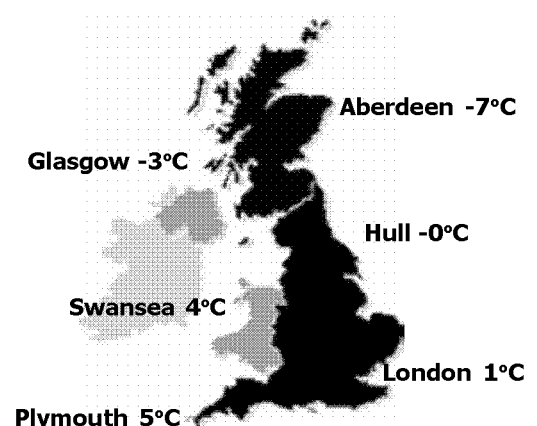
Write the temperature given by each thermometer. The first one is done for you.



10°C

Now look at the map of Britain and answer the questions.

- Which city has the warmest temperature?
- How many degrees below freezing is Glasgow?
- How many degrees above freezing is Swansea?
- Is Aberdeen colder than Glasgow?
- Which city has the coldest temperature?



### 3.3 Addition and Subtraction

We use these rules when we add and subtract with negative numbers:

$+(+2) = 2$	$- (+2) = -2$
$+ (-2) = -2$	$- (-2) = 2$

**Example - Find  $5 + (-7)$**

$$5 + (-7) = 5 - 7 = -2$$

**Example - Find  $3 - (-2) + (-8) + 1$**

$$3 - (-2) + (-8) + 1 = 3 + 2 - 8 + 1 = -2$$

#### Practice

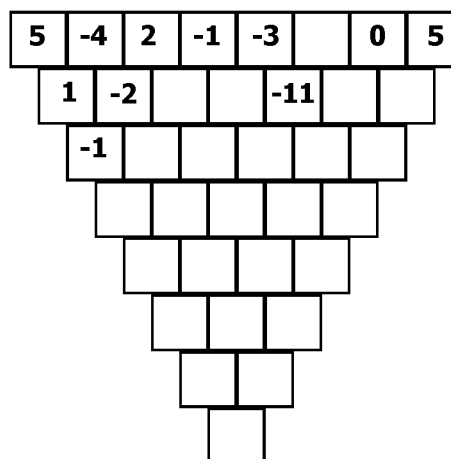
i. Find:

- |                           |                       |
|---------------------------|-----------------------|
| a) $3 + (-6)$             | f) $12 + (+8) - (-4)$ |
| b) $-2 - (-3)$            | g) $2 - (-4) + 6$     |
| c) $-5 - (+7)$            | h) $-2 - (+12)$       |
| d) $- (+1) - (+5)$        | i) $-9 + (-2) - (-3)$ |
| e) $- (+3) + (+5) - (+5)$ |                       |

ii. Find the following. Remember, brackets first!

- a)  $3 - (4 - 3)$   
 b)  $6 + (8 - 15)$   
 c)  $5 + (7 - 9)$   
 d)  $5 - (6 - 10)$   
 e)  $(4 - 8) - (10 - 15)$   
 f)  $(3 - 8) - (9 - 4)$

iii. The numbers in this triangle are found by adding together the two numbers above. Complete it.



### 3.4 Multiplication and Division

We already know that  $4 \times 2 = 8$  and that  $4 \div 2 = 2$ . For negative numbers we use these rules:

If one number is negative, the answer is negative:

$$(-3) \times 2 = -6 \text{ and } 3 \times (-2) = -6$$

$$4 \div (-2) = -2 \text{ and } (-4) \div 2 = -2$$

If both numbers are negative, the answer is positive:

$$(-3) \times (-2) = 6$$

$$(-4) \div (-2) = 2.$$

#### Practice

Find:

- |                    |                    |                    |                       |                         |                        |
|--------------------|--------------------|--------------------|-----------------------|-------------------------|------------------------|
| a) $6 \times (-4)$ | b) $7 \times (-2)$ | c) $8 \times (-2)$ | d) $(-8) \times (-3)$ | e) $(-12) \times (-11)$ | f) $(-16) \times (-7)$ |
| g) $(-6) \div 2$   | h) $(-15) \div 3$  | i) $(-28) \div 7$  | j) $(-28) \div (-4)$  | k) $(-72) \div (-9)$    | l) $(-144) \div (-12)$ |

**Why does a negative number multiplied by a negative number give a positive answer?**

First, we use some things we already know:

$$3 + (-3) = 0 \text{ and } 2 \times (0) = 0.$$

These tell us that:

$$2 \times (0) = 2 \times (3 + (-3)) = 0.$$

We can **expand** the brackets:

$$2 \times (3 + (-3)) = 2 \times 3 + 2 \times (-3).$$

So:

$$2 \times (0) = 2 \times 3 + 2 \times (-3) = 6 + 2 \times (-3) = 0.$$

For this to be true,  $2 \times (-3)$  must be equal to  $-6$  so:

$$2 \times (0) = 6 + (-6) = 6 - 6 = 0.$$

*From this example we learn that a negative multiplied by a positive gives a negative answer.*

However, it is also true that  $-2 \times (0) = 0$  and that  $-2 \times (0) = -2 \times (3 + (-3)) = -2 \times 3 + (-2) \times (-3) = 0$ .

We already know that  $-2 \times 3 = -6$ . So,  $-2 \times (0) = -6 + (-2) \times (-3) = 0$ .

This is only true if  $(-2) \times (-3)$  is equal to  $6$  so that  $-2 \times (0) = -6 + 6 = 0$ .

*From this example we learn that a negative multiplied by a negative gives a positive answer.*

# 4. Decimals

## 4.1 Introduction

The **decimal point** separates the whole numbers from the parts of the whole.

### Think

**units**    **tenths**    **hundredths**    **thousandths**  
**8**    •    **4**       **7**       **5**

The number in the **tenths** column is 4. There are 4 tenths. In decimal notation this is 0.4

How many **hundredths** are there? **Thousandths**?  
 Can you write these as decimals?  
 Do you know how to say this number?

### Practice

i. Practice saying these numbers

- a) 0.8725                      c) 72.156874  
 b) 24.9182                    d) 0.05146

ii. Write the underlined digits in words.

iii. Write these as decimal numbers

- a) fifteen, three tenths and four hundredths  
 b) eleven and seven hundredths  
 c) twenty seven and thirty five thousandths  
 d) five tenths and six thousandths

## 4.2 Addition of Decimals

We add decimals in the same way we add whole numbers.

**Example - Find  $5.3 + 6.8$**

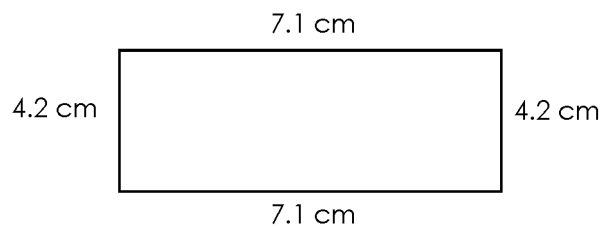
$$\begin{array}{r} 5.3 \\ + 6.8 \\ \hline 12.1 \end{array}$$

### Practice

i. Solve the following

- a)  $7.2 + 3.6$                       e)  $4.62 + 0.078$   
 b)  $0.013 + 0.026$               f)  $0.32 + 0.032 + 0.0032$   
 c)  $3.87 + 0.11$                   g)  $7.34 + 6 + 14.034$   
 d)  $0.0043 + 0.263$

ii. Find the **perimeter** of the **rectangle**  
 (perimeter is the distance all the way around):



**Activity** - Copy the grid of numbers into your exercise book

4.33	0.59	2.36	5.608	3.182	0.57	0.649
6.25	1.89	5.81	3.218	1.14	2.98	3.902
3.722	0.9	3.7	5.959	6.27	6.804	0.098
0.13	5.91	3.241	0.68	1.291	2.99	4.2

Cross out pairs of numbers that add up to between 5 and 7 (for example  $4.33 + 1.89 = 6.22$ ).  
 You have 2 minutes to cross out as many pairs as possible.

Your score is the sum of all the remaining numbers.

The person with the lowest score is the winner.

Try again with your partner to reduce your score. What is the lowest possible score?

## 4.3 Subtraction of Decimals

We also subtract decimals in the same way we subtract whole numbers.

**Example - Find  $24.2 - 13.7$**

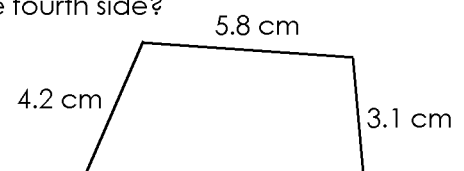
$$\begin{array}{r} 24.2 \\ - 13.7 \\ \hline 10.5 \end{array}$$

### Practice

i. Solve the following:

- a)  $9.6 - 1.8$                       e)  $11 - 8.6$   
 b)  $17.23 - 0.36$                 f)  $0.73 - 0.0006$   
 c)  $7.063 - 0.124$                 g)  $9.2 + 13.21 - 14.6$   
 d)  $3.2 - 0.26$

ii. The perimeter of the shape is 19 cm.  
 What is the length of the fourth side?

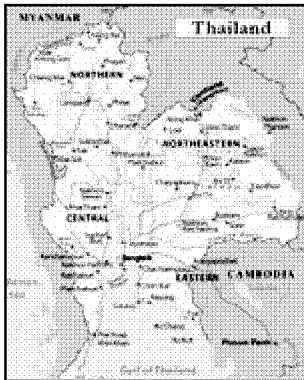


## 4.4 Changing Units - Length

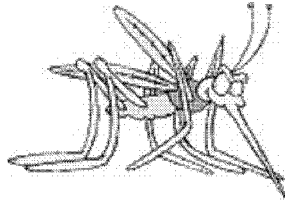
The metric units of length are kilometre (km), metre (m), centimetre (cm) and millimetre (mm).

### Think

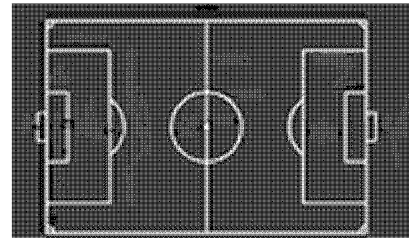
Which unit of length is used to measure the following:



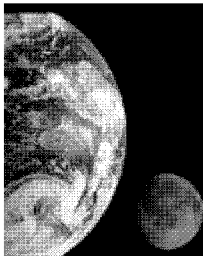
a) The distance between Mae Sot and Bangkok?



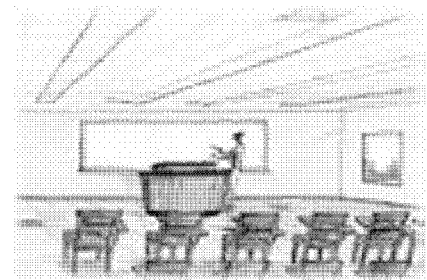
c) The length of a mosquito?



b) The length of a football pitch?



The distance to the moon is measured in kilometres.  
Can you guess how far it is?



d) The width of your classroom?

To compare lengths we write them with the same units. We use the following relationships:

$1 \text{ km} = 1000 \text{ m}$	$1 \text{ m} = 100 \text{ cm}$
$1 \text{ m} = 1000 \text{ mm}$	$1 \text{ cm} = 10 \text{ mm}$

To change from large units to small units we use multiplication.

To change from small units to large units we use division.

**Example -** Write 3.5 m in centimetres.

Use  $1 \text{ m} = 100 \text{ cm}$

$$3.5 \text{ m} = 3.5 \times 100 \text{ cm} = 350 \text{ cm}.$$

**Example -** Write 580 m in kilometres.

Use  $1 \text{ km} = 1000 \text{ m}$

$$580 \text{ m} = 580 \div 1000 \text{ km} = 0.58 \text{ km}.$$

### Practice

i. Write the quantity in the smaller units given in brackets:

a) 2 m (cm)

b) 3 cm (mm)

c) 1.5 m (cm)

d) 9.2 m (mm)

e) 2 km (mm)

ii. Write the quantity in the larger units given in brackets:

a) 300 mm (cm)

b) 150 cm (m)

c) 12 cm (m)

d) 1250 mm (m)

e) 2850 m (km)

## 4.5 Changing Units - Mass

The metric units of mass are tonne (t), kilogram (kg) and gram (g) and milligram (mg).

We use the following relationships:

$1 \text{ t} = 1000 \text{ kg}$	$1 \text{ kg} = 1000 \text{ g}$	$1 \text{ g} = 1000 \text{ mg}$
---------------------------------	---------------------------------	---------------------------------

We use grams and kilograms for things we use everyday. We use tonnes for heavier things.

## Think

Which unit of mass is used to weigh:



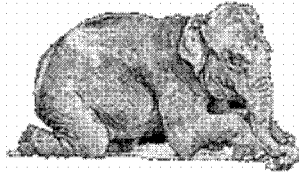
a) Your friend?



c) A jar of coffee?



b) A truck?



d) 100 elephants?

We change units in the same way as before.

**Example -** Write 2.35 t in grams.

$$2.35 \text{ t} = 2.35 \times 1000 \text{ kg} = 2350 \text{ kg}$$

$$2350 \times 1000 \text{ g} = 2,350,000 \text{ g}$$

First we change tonnes to kilograms.

Then we change kilograms to grams.

## Practice

i. Write the quantity in the smaller units given in brackets:

a) 12 t (kg)

d) 0.7 t (g)

b) 13 kg (g)

e) 0.72 kg (mg)

c) 0.3 g (mg)

ii. Write the quantity in the larger units given in brackets:

a) 1500 g (t)

d) 190 kg (t)

b) 1500 mg (g)

e) 86 g (kg)

c) 5020 g (kg)

## 4.6 Adding and Subtracting Quantities

To add or subtract two or more quantities they must have the same units.

### Think

How do we change to kilograms?

**Example -** Write 1 kg + 158 g in grams.

$$1 \text{ kg} = 1000 \text{ g.}$$

$$1 \text{ kg} + 158 \text{ g} = 1000 \text{ g} + 158 \text{ g} = 1158 \text{ g.}$$

d) 52 mg + 87 g (kg)

e) 3.9 m + 582 mm (cm)

f) 20 g - 150 mg (g)

### Practice

i. Solve the following giving your answer in the unit given in brackets:

a) 5 m + 86 cm (m)

b) 36 cm - 87 mm (m)

c) 116 g + 0.93 kg (g)

ii. Solve the following:

a) Aung Aung goes to the market and buys 2 kg of potatoes, 250 g of coffee and 600 g of beans. What is the total weight in kilograms?

b) To visit his friend in Mae Sot Min Thaw walks 900m to the road and then travels 32.65 km by linecar. His friend's house is 450 m from the bus station. How far does he travel in kilometres?

## 4.7 Multiplying Decimals by Whole Numbers

We multiply a decimal number and a whole number in the same way as we multiply two whole numbers.

**Example -** Find  $2.68 \times 31$

$$\begin{array}{r} 2.68 \\ \times 31 \\ \hline 164.08 \\ 80.40 \text{ — Don't forget to add the zero.} \\ \hline 96.48 \end{array}$$

### Think

How do we order the quantities, 45 cm, 0.4 m, 360 mm and 0.002 km? What do we do first?

### Practice

Calculate the following:

a)  $812.9 \times 4$

e)  $812.9 \times 43$

b)  $0.126 \times 4$

f)  $0.126 \times 47$

c)  $9 \times 1.43$

g)  $92 \times 1.43$

d)  $53.72 \times 6$

h)  $53.72 \times 64$

i) Some students have to build a new wall for the classroom using bamboo. They need 23 pieces of bamboo that are 3.67 m long. What is the total length of bamboo needed?

## 4.8 Dividing Decimals by Whole Numbers

We also divide a decimal number and a whole number in the same way as we divide two whole numbers.

**Example - Find  $0.45 \div 5$**

$$\begin{array}{r} 0.09 \\ 5 \overline{)0.45} \end{array} \quad (5 \times 9 = 45)$$

5 does not go into 4 so we write a zero in the tenths column.

**Example - Find  $4.2 \div 25$**

$$\begin{array}{r} 0.168 \\ 25 \overline{)4.200} \\ \underline{25} \phantom{00} \\ 170 \phantom{0} \\ \underline{150} \phantom{0} \\ 200 \\ \underline{200} \phantom{0} \end{array}$$

### Practice

i. Calculate the following:

a)  $0.672 \div 3$

b)  $26.6 \div 7$

c)  $0.6552 \div 6$

d)  $0.0285 \div 5$

e)  $9.45 \div 21$

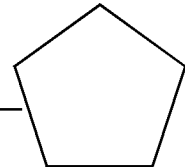
f)  $0.864 \div 24$

g)  $71.76 \div 23$

h)  $0.2585 \div 25$

ii. A **pentagon** is a 5-sided shape. The perimeter of the pentagon shown is 16.24 cm. What is the length of one side?

All the sides are equal



## 4.9 Multiplying Decimals

### Think

Earlier we learnt that  $0.2 = 2 \div 10$ . How can we use this to calculate  $0.3 \times 0.2$ ?

### Practice

Calculate the following:

a)  $0.04 \times 0.2$

b)  $0.003 \times 0.1$

c)  $0.3 \times 0.002$

d)  $0.7 \times 0.001$

e)  $0.07 \times 0.008$

f)  $8 \times 0.6$

g)  $0.2 \times 0.008$

h)  $4 \times 0.0009$

Compare the number of the **decimal places** in the answer with the those in the numbers being multiplied. What do you notice?

**Example - Find  $0.08 \times 0.4$**

$$8 \times 4 = 32$$

$$\begin{array}{rcccl} 0.08 & \times & 0.4 & = & 0.032 \\ (2 \text{ places}) & & (1 \text{ place}) & & (3 \text{ places}) \end{array}$$

**Example - Find  $0.252 \times 0.4$**

$$\begin{array}{r} 252 \\ \times 4 \\ \hline 1008 \end{array}$$

$$\begin{array}{rcccl} 0.252 & \times & 0.4 & = & 0.1008 \\ (3 \text{ places}) & & (1 \text{ place}) & & (4 \text{ places}) \end{array}$$

### Practice

Calculate the following:

a)  $0.751 \times 0.2$

b)  $5.6 \times 0.02$

c)  $0.16 \times 0.005$

d)  $0.5 \times 0.005$

e)  $310 \times 0.04$

f)  $0.68 \times 0.543$

g)  $1.36 \times 0.082$

h)  $0.0072 \times 0.034$



## 4.10 Division by Decimals

**Example** - Calculate  $0.012 \div 0.06$

$0.012 \div 0.06$  can be written as  $\frac{0.012}{0.06}$

$$\frac{0.012}{0.06} = \frac{0.012 \times 100}{0.06 \times 100}$$

$$= \frac{1.2}{6}$$

$$= 0.2$$

Multiplying top and bottom by the same number does not change the value.

It is easier to divide by a whole number.

This is the answer!

### Practice

Calculate the following:

a)  $0.48 \div 0.04$

b)  $3.6 \div 0.06$

c)  $0.84 \div 0.07$

d)  $0.168 \div 0.014$

e)  $20.8 \div 0.0004$

f)  $0.00132 \div 0.11$

g)  $4.96 \div 1.6$

h)  $0.0204 \div 0.017$

## 4.11 Decimal Places

We already know how to round whole numbers. We round to a given number of **decimal places (d.p.)** in a similar way.

### Think

Look at the number on the right. How do we round it to 1 d.p.? What about 2 d.p.?

4 3 . 0 5 7  
1st 2nd 3rd  
decimal place

### Practice

i. Round the following to the nearest whole number:

a) 13.9

b) 109.7

c) 152.4

d) 0.98

ii. Round the following to the number of decimal places given in brackets:

a) 1.2671 (2 d.p.)

b) 0.0416 (3 d.p.)

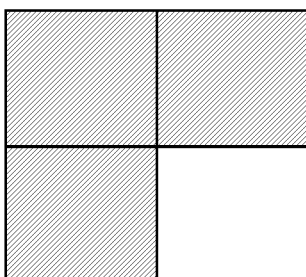
c) 3.9949 (2 d.p.)

d) 8.0293 (2 d.p.)

iii. Look at the division questions i. in Section 4.8. Round your answers to 2 d.p.

# 5. Fractions

## 5.1 Introduction



### Think

How many parts is the square divided into?

How many parts are shaded?

Do you know how to write this as a fraction?

**Numerator**

\_\_\_\_\_

**Denominator**

The bottom number in a fraction is the total number of parts. It is called the **denominator**.

The top number is the number of parts we are counting. It is called the **numerator**.

The fraction above is called a **proper fraction** because the numerator is *less than* the denominator.

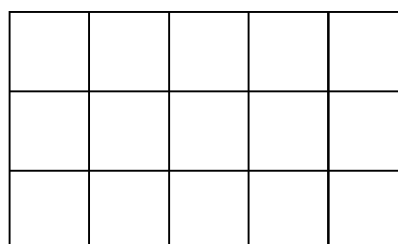
## Practice

- i. There are 60 minutes in one hour. What fraction of an hour is:
- a) 1 minute?      b) 7 minutes?      c) 35 minutes?      d) 55 minutes?
- ii. You go to school 5 days every week. What fraction of the week are you at school?
- iii. To travel from Mandalay to Mawlamyine I take a train to Rangoon which costs \$35, then I take a bus to Moulmein for \$9. What fraction of the total cost is the bus to Mawlamyine?
- iv. Which subject do you like most, Maths, English or Social Studies? Complete the table after the class has voted.

Maths	English	Social Studies	Total

What fraction of the class like Maths the most? What about English and Social Studies?

- v. Naw Kaw prepared an area for a vegetable garden. Using rope she divided the area into 15 equal squares. What fraction of the whole garden is given by one square? She planted corn in 3 squares and green beans in 2 squares. Shade these squares on the diagram. What fraction of the whole garden has been planted?



## 5.2 Improper Fractions and Mixed Numbers

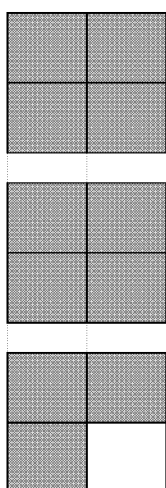
If the numerator is greater than the denominator then the fraction is an **improper fraction**.

In the diagram one square is made of 4 parts. There are 11 shaded parts in total, so we write:  $\frac{11}{4}$

An improper fraction can also be written as a **mixed number** - part whole number and part fraction. In the diagram there are 2 whole squares and  $\frac{3}{4}$  of another square shaded, so we write:  $2\frac{3}{4}$

$$\frac{11}{4}$$

improper fraction



$$2\frac{3}{4}$$

mixed number

### Think

What do we learn about  $\frac{11}{4}$  and  $2\frac{3}{4}$  from this example?

**Activity** - Write some examples of proper fractions, improper fractions and mixed numbers below. Show them to your partner and ask him/her to classify them.

We can write mixed numbers as improper fractions and improper fractions as mixed numbers.

**Example** - Write  $3\frac{5}{8}$  as an improper fraction.

$$3 = \frac{3 \times 8}{8} = \frac{24}{8}. \quad 3\frac{5}{8} = \frac{24}{8} + \frac{5}{8} = \frac{29}{8}.$$

**Example** - Write  $\frac{32}{5}$  as a mixed number.

Divide 32 by 5:  $5 \overline{)32} 6 \text{ remainder } 2$ .

In words, this is 6 wholes and 2 parts. So,  $\frac{32}{5} = 6\frac{2}{5}$ .

## Practice

Write the improper fractions as mixed numbers:

i. a)  $\frac{11}{5}$       b)  $\frac{12}{7}$       c)  $\frac{27}{8}$       d)  $\frac{84}{9}$       e)  $\frac{91}{6}$       f)  $\frac{121}{9}$

Write the mixed numbers as improper fractions:

ii. a)  $2\frac{3}{4}$       b)  $4\frac{1}{6}$       c)  $3\frac{11}{15}$       d)  $7\frac{5}{12}$       e)  $4\frac{7}{9}$       f)  $10\frac{3}{7}$

## 5.3 Equivalent Fractions

### Think

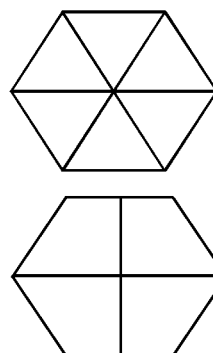
Shade 3 parts of the first shape and 2 parts of the second.

What do you see?

Look at the shapes and complete the statement: \_\_\_\_\_ = \_\_\_\_\_

The fractions above are **equivalent**. They have the same value.

Equivalent sets of fractions can be found using a **multiplication wall**.



1	2	3	4	5	6	7	8	9	10
2	4	6	8	10	12	14	16	18	20
3	6	9	12	15	18	21	24	27	30
4	8	12	16	20	24	28	32	36	40
5	10	15	20	25	30	35	40	45	50
6	12	18	24	30	36	42	48	54	60

### Think

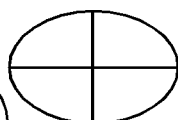
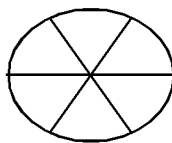
Look at the 2nd and 5th rows of the multiplication wall. Complete the set of equivalent fractions:

$$\frac{2}{5} = \frac{4}{10} =$$

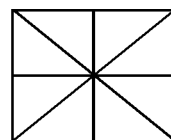
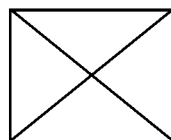
## Practice

Shade the shapes to show that the fractions are equivalent

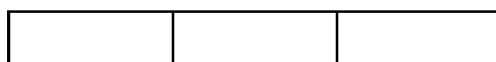
a)  $\frac{1}{3} = \frac{2}{6}$



b)  $\frac{2}{4} = \frac{4}{8}$



c)  $\frac{2}{3} = \frac{8}{12}$

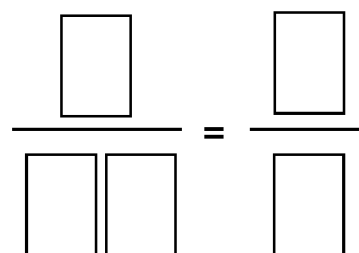


Use the multiplication wall to make sets of equivalent fractions for **a)**, **b)** and **c)**.

**Activity -** For this you need nine pieces of paper numbered 1-9.

Investigate different ways of placing the numbers on the diagram to make equivalent fractions.

Start by keeping one of the denominators the same and changing the other 3 numbers to make equivalent fractions.



**Example** - Find the equivalent fraction:  $\frac{3}{8} = \frac{\quad}{40}$

The denominator has been multiplied by 5.

We multiply the numerator by the same value:

$$\frac{3}{8} = \frac{3 \times 5}{8 \times 5} = \frac{15}{40}$$

The missing number is 15.

## Practice

Complete these pairs of equivalent fractions

a)  $\frac{1}{6} = \frac{\quad}{18}$

b)  $\frac{3}{7} = \frac{\quad}{14}$

c)  $\frac{3}{8} = \frac{\quad}{48}$

d)  $\frac{5}{6} = \frac{\quad}{36}$

e)  $\frac{4}{9} = \frac{24}{\quad}$

f)  $\frac{5}{7} = \frac{\quad}{56}$

g)  $\frac{8}{9} = \frac{40}{\quad}$

h)  $\frac{7}{12} = \frac{84}{\quad}$

i)  $\frac{7}{8} = \frac{49}{\quad}$

## 5.4 Simplifying Fractions

We can **simplify** a fraction by finding **common factors** of the numerator and the denominator.

**Example** - Write  $\frac{32}{56}$  in its simplest form.

$32 = 4 \times 8$  and  $56 = 7 \times 8$ . 8 is a common factor.

$$\frac{32}{56} = \frac{4 \times 8}{7 \times 8} = \frac{4}{7}$$

**Cancelling** the 8s gives the answer.

$\frac{4}{7}$  is  $\frac{32}{56}$  written in its **lowest terms**.

**Example** - What fraction of 1 m is 35 cm?

$$100 \text{ cm} = 1 \text{ m, so } 35 \text{ cm} = \frac{35}{100} \text{ m} = \frac{7}{20} \text{ m}$$

Remember to simplify your answer!

## Practice

i. Simplify the fractions:

a)  $\frac{6}{10}$

b)  $\frac{12}{18}$

c)  $\frac{42}{66}$

d)  $\frac{132}{144}$

e)  $\frac{54}{162}$

f)  $\frac{49}{77}$

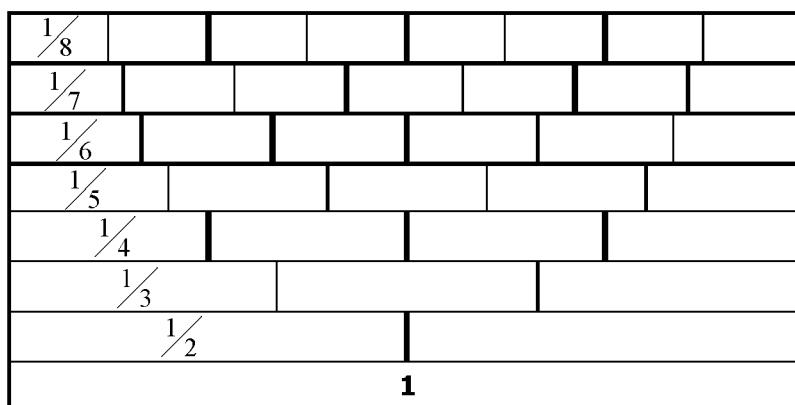
ii. Write the answer in its lowest terms:

a) What fraction of a kilogram is 24 grams?

b) How many days are there in 60 hours?

## 5.5 Ordering Fractions

We can use a **fraction wall** to compare fractions with different denominators.



## Think

Look at the wall. Which fraction is bigger,  $\frac{1}{2}$  or  $\frac{1}{3}$ ? How about  $\frac{1}{4}$  and  $\frac{1}{7}$ ?

Is this statement true:  $\frac{3}{4} > \frac{2}{3}$ . How can you use the wall to find out?

We can order sets of fractions by writing them all with a **common denominator**. A set of fractions has a common denominator if their denominators are all the same.

**Example -** Order  $\frac{1}{2}, \frac{7}{10}, \frac{3}{4}, \frac{3}{5}$

Find a common denominator for the fractions:

$$\frac{1}{2} = \frac{1 \times 10}{2 \times 10} = \frac{10}{20}, \quad \frac{7}{10} = \frac{7 \times 2}{10 \times 2} = \frac{14}{20}, \quad \frac{3}{4} = \frac{3 \times 5}{4 \times 5} = \frac{15}{20}, \quad \frac{3}{5} = \frac{3 \times 4}{5 \times 4} = \frac{12}{20}$$

By comparing the numerators we see that the order is:

$$\frac{10}{20}, \frac{12}{20}, \frac{14}{20}, \frac{15}{20} \text{ or } \frac{1}{2}, \frac{3}{5}, \frac{7}{10}, \frac{3}{4}.$$

20 is a common denominator for these fractions.

## Practice

i. Use the fraction wall to write the correct symbol  $>$  or  $<$  between the two fractions:

a)  $\frac{1}{4}$     $\frac{1}{7}$

b)  $\frac{1}{2}$     $\frac{7}{10}$

c)  $\frac{5}{6}$     $\frac{3}{8}$

d)  $\frac{3}{7}$     $\frac{32}{56}$

ii. Find which fraction is bigger by writing them with common denominators:

a)  $\frac{3}{4}$  or  $\frac{5}{6}$

b)  $\frac{9}{11}$  or  $\frac{7}{9}$

c)  $\frac{5}{6}$  or  $\frac{3}{8}$

d)  $\frac{5}{7}$  or  $\frac{7}{9}$

iii. Order each set of fractions. Start with the smallest:

a)  $\frac{17}{28}, \frac{3}{4}, \frac{11}{14}, \frac{5}{7}$

b)  $\frac{7}{12}, \frac{2}{3}, \frac{17}{24}, \frac{3}{4}$

c)  $\frac{13}{20}, \frac{3}{4}, \frac{4}{10}, \frac{5}{8}$

## 5.6 Changing Fractions to Decimals

We can write fractions as decimals by finding an equivalent fraction with a denominator of 10, 100, 1000....

**Example -** Write  $\frac{2}{5}$  as a decimal.

$$\frac{2}{5} = \frac{4}{10} = \text{four tenths} = 0.4.$$

**Example -** Write  $3\frac{3}{4}$  as a decimal.

$$\frac{3}{4} = \frac{75}{100} = \text{seventy five hundredths} \\ = \text{seven tenths and five hundredths} = 0.75.$$

$$3\frac{3}{4} = 0.75$$

**Example -** Write  $\frac{3}{8}$  as a decimal.

$$\frac{3}{8} \text{ means } 3 \div 8 \text{ and } 8 \overline{)3.000}.$$

$$\text{So, } \frac{3}{8} = 0.375.$$

We use division because we cannot write the fraction with a denominator of 10, 100.....

## Think

We can also write decimals as fractions. Can you write 0.2, 0.75 and 0.05 as fractions?

## Practice

i. Write each fraction as a decimal:

a)  $\frac{2}{5}$

b)  $\frac{1}{4}$

c)  $2\frac{4}{25}$

d)  $\frac{5}{16}$

e)  $1\frac{7}{8}$

ii. Write each pair of fractions as decimals and put the correct symbol  $>$  or  $<$  between them:

a)  $\frac{2}{5}$     $\frac{1}{2}$

b)  $\frac{8}{10}$     $\frac{3}{4}$

c)  $\frac{8}{10}$     $\frac{22}{25}$

d)  $\frac{3}{20}$     $\frac{2}{25}$

iii. Write each decimal as a fraction. Write the fraction in its lowest terms:

a) 0.3

b) 0.42

c) 2.78

d) 7.12

e) 0.325

iv. Order each set by writing them as decimals:

a)  $\frac{1}{2}, 0.26, \frac{1}{4}, 0.3, \frac{31}{100}$

b)  $0.91, \frac{4}{5}, \frac{19}{20}, 0.85$

c)  $1\frac{3}{4}, 1.35, 1\frac{7}{10}, 1.4, 1\frac{16}{20}$

v. Order each set of measurements, starting with the largest:

a) 4.101 m, 4.009 m, 4.0059 m

b)  $\frac{1}{8}$  kg, 0.55 kg, 0.525 kg, 1.25 kg

c)  $9\frac{9}{10}$  tonnes, 9.904 tonnes, 9.804 tonnes, 9.99 tonnes

d) 2.02 litres,  $\frac{1}{5}$  litres, 2.0 litres, 0.022 litres

## 5.7 Fractions as Recurring Decimals

### Think

In the above example we used division to show that  $\frac{3}{8} = 0.375$ . Use the same method to change  $\frac{2}{3}$  and  $\frac{2}{7}$  into decimals. Write your answers below to 12 decimal places. What do you notice?

A number or group of numbers that repeats like this is called a **recurring decimal**.

We use a dot above the figures that **recur**:

$$\frac{2}{3} = 0.66666666 = 0.\dot{6} \quad \frac{2}{7} = 0.285714285714 = 0.\dot{2}8571\dot{4}$$

### Practice

Write the fractions as recurring decimals. Use dots to show how each decimal recurs

a)  $\frac{4}{9}$

b)  $\frac{2}{11}$

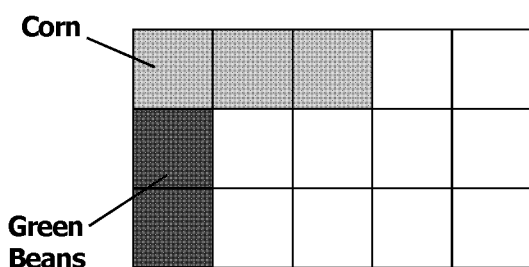
c)  $\frac{7}{9}$

d)  $\frac{8}{7}$

## 5.8 Adding and Subtracting Fractions

### Think

This week Naw Kaw planted Betel nut in four squares of her garden. Shade this area on the diagram. What fraction of her garden is now planted? Express this in its simplest form.



Fractions with the same denominator are added or subtracted by adding or subtracting the numerators. If fractions have different denominators, then we write them as equivalent fractions.

**Example -**  $\frac{5}{15} + \frac{4}{15} = \frac{9}{15} = \frac{3}{5}$   
 $\frac{8}{15} - \frac{3}{15} = \frac{5}{15} = \frac{1}{3}$

**Example -**  $\frac{2}{3} - \frac{1}{5} = \frac{10}{15} - \frac{3}{15} = \frac{7}{15}$

**To add or subtract mixed numbers we follow these steps:**

1. Change to improper fractions
2. Change to equivalent fractions with a common denominator.
3. Add or subtract.
4. Write the answer in its simplest form.

### Practice

i. Solve and write the answer in its lowest terms

a)  $\frac{3}{5} + \frac{1}{5}$

b)  $\frac{5}{8} + \frac{2}{8}$

c)  $\frac{5}{16} + \frac{7}{16}$

d)  $\frac{33}{99} + \frac{11}{99} + \frac{22}{99} + \frac{33}{99}$

ii. The following fractions have different denominators. Solve and write the answer in its lowest terms

a)  $\frac{2}{5} + \frac{1}{6}$       b)  $\frac{3}{7} + \frac{1}{6}$       c)  $\frac{3}{10} + \frac{2}{3}$       d)  $\frac{3}{11} + \frac{5}{9}$       e)  $\frac{3}{8} + \frac{7}{16}$       f)  $\frac{3}{12} + \frac{1}{6}$   
 g)  $\frac{5}{12} + \frac{1}{6} + \frac{1}{3}$       h)  $\frac{3}{10} + \frac{1}{5} + \frac{1}{4}$

iii. Subtract and write the answer in its lowest terms

a)  $\frac{8}{9} - \frac{2}{9}$       b)  $\frac{3}{4} - \frac{1}{4}$       c)  $\frac{2}{3} - \frac{3}{7}$       d)  $\frac{8}{11} - \frac{2}{5}$       e)  $\frac{8}{13} - \frac{1}{2}$       f)  $\frac{66}{99} - \frac{22}{99} - \frac{33}{99} - \frac{11}{99}$

iv. Solve and write the answer in its lowest terms

a)  $\frac{7}{12} - \frac{1}{6} + \frac{1}{3}$       b)  $\frac{5}{8} - \frac{21}{40} + \frac{2}{5}$       c)  $\frac{3}{8} + \frac{7}{16} - \frac{3}{4}$       d)  $\frac{13}{16} - \frac{1}{8} + \frac{3}{4}$

v. Follow the steps above to add or subtract the mixed numbers

a)  $1\frac{1}{8} + \frac{3}{8}$       b)  $2\frac{7}{10} - \frac{3}{10}$       c)  $1\frac{3}{4} + 2\frac{3}{4}$       d)  $3\frac{1}{5} - 2\frac{2}{5}$   
 e)  $2\frac{1}{4} + 3\frac{1}{2}$       f)  $5\frac{5}{9} - 4\frac{1}{3}$       g)  $8\frac{4}{7} - 2\frac{1}{3}$

vi. Solve these problems.

a) Tin Tin adds two fractions. How many mistakes did he make? Explain the mistakes.

$$\frac{1}{4} + \frac{2}{5} = \frac{5}{20} + \frac{4}{20} = \frac{9}{40}$$

b) Every day Saw Saw spends  $\frac{1}{3}$  of his time sleeping,  $\frac{1}{4}$  of his time at school and  $\frac{1}{12}$  of his time eating. What fraction of the day is remaining?

c) Naw Kaw's garden is  $6\frac{1}{4}$  m wide and  $5\frac{3}{4}$  m long. What is the perimeter of her garden?

d) At the end of the rainy season she harvested her crops. She had  $5\frac{1}{2}$  kg of corn,  $2\frac{1}{4}$  kg of green beans and 7 kg of cucumber. What was the total weight of her harvest? Write the answer as a fraction and as a decimal.

### Activity - Egyptian Fractions

A unit fraction is a fraction with a denominator of 1,  $\frac{1}{3}$ ,  $\frac{1}{5}$  and  $\frac{1}{7}$  are unit fractions.

The Egyptians only used unit fractions. The Egyptians wrote  $\frac{7}{20}$  by adding unit fractions:

$$\frac{7}{20} = \frac{4}{20} + \frac{2}{20} + \frac{1}{20} = \frac{1}{5} + \frac{1}{10} + \frac{1}{20}$$

Work with a partner to write  $\frac{13}{20}$  as the sum of unit fractions. Write some more proper fractions as the sums of unit fractions. Can you calculate  $\frac{7}{20} + \frac{13}{40}$  using the Egyptian method?

## 5.9 Multiplying Fractions

We multiply fractions by multiplying the numerators and denominators:

$$\frac{1}{2} \times \frac{1}{4} = \frac{1 \times 1}{2 \times 4} = \frac{1}{8}$$

Look at the diagram. The shaded region is  $\frac{1}{2}$  of  $\frac{1}{4}$  the shape.

It is also  $\frac{1}{8}$  of the total shape. We see that  $\frac{1}{2}$  of  $\frac{1}{4} = \frac{1}{8}$ .



**We have  $\frac{1}{2} \times \frac{1}{4} = \frac{1}{8}$  and  $\frac{1}{2}$  of  $\frac{1}{4} = \frac{1}{8}$ . We learn that 'of' means 'multiplied by'.**

This helps us find fractions of whole numbers and quantities.

**Example -** Find three fifths of 95 metres.

$$\frac{3}{5} \text{ of } 95 = \frac{3}{5} \times 95 = \frac{3}{5} \times \frac{95}{1} = \frac{3}{5 \times 1} \times \frac{5 \times 19}{1}$$

$$= \frac{3}{1} \times \frac{19}{1} = 3 \times 19 = 57.$$

So, three fifths of 95 metres is 57 metres.

Notice that we can write 95 as a fraction with a denominator of 1 to make the calculation easier:

$$95 = \frac{95}{1} = 95 \div 1 = 95$$

We can cancel the 5's.

## Practice

i. Draw diagrams to show that

a)  $\frac{1}{2}$  of  $\frac{1}{3} = \frac{1}{6}$

b)  $\frac{1}{3}$  of  $\frac{1}{2} = \frac{1}{6}$

c)  $\frac{2}{3}$  of  $\frac{1}{3} = \frac{2}{9}$

d)  $\frac{1}{4}$  of  $\frac{1}{3} = \frac{1}{12}$

ii. Find

a)  $\frac{1}{3}$  of 18

b)  $\frac{1}{5}$  of 30

c)  $\frac{3}{8}$  of 64

d)  $\frac{3}{5}$  of 20 metres

e)  $\frac{1}{4}$  of 200 baht

f)  $\frac{1}{7}$  of 1 week

g)  $\frac{3}{7}$  of 35 km

h)  $\frac{7}{8}$  of 1 day (24 hours)

When we multiply two fractions we look for common factors of the numerators and denominators.

**Example -** Find  $\frac{4}{25} \times \frac{15}{16}$

We can cancel 4 with 16 and 5 with 25 to get:

$$\frac{4}{25} \times \frac{15}{16} = \frac{1}{25} \times \frac{15}{4} = \frac{1}{5} \times \frac{3}{4} = \frac{1 \times 3}{5 \times 4} = \frac{3}{20}$$

**Example -** Find  $\frac{3}{5} \times \frac{15}{16} \times \frac{4}{7}$

We cancel 5 with 15 and 16 with 4 to get:

$$\frac{3}{5} \times \frac{15}{16} \times \frac{4}{7} = \frac{3}{1} \times \frac{3}{16} \times \frac{4}{7} = \frac{3}{1} \times \frac{3}{4} \times \frac{1}{7} = \frac{3 \times 3 \times 1}{1 \times 4 \times 7} = \frac{9}{28}$$

## Practice

i. Find

a)  $\frac{3}{4} \times \frac{1}{2}$

b)  $\frac{2}{3} \times \frac{5}{7}$

c)  $\frac{1}{2} \times \frac{7}{8}$

d)  $\frac{3}{4} \times \frac{1}{5}$

e)  $\frac{1}{7} \times \frac{3}{5}$

ii. Cancel the common factors to find

a)  $\frac{7}{8} \times \frac{4}{21}$

b)  $\frac{3}{4} \times \frac{16}{21}$

c)  $\frac{48}{55} \times \frac{5}{12}$

d)  $\frac{4}{15} \times \frac{25}{64}$

e)  $\frac{3}{7} \times \frac{28}{33}$

f)  $\frac{3}{7} \times \frac{5}{9} \times \frac{14}{15}$

g)  $\frac{15}{16} \times \frac{8}{9} \times \frac{4}{5}$

h)  $\frac{3}{10} \times \frac{5}{9} \times \frac{6}{7}$

i)  $\frac{7}{16} \times \frac{8}{21} \times \frac{9}{11}$

iii. The following questions contain mixed numbers. Solve by changing them to improper fractions and then cancelling common factors

a)  $1\frac{2}{5} \times \frac{2}{5}$

b)  $1\frac{1}{4} \times \frac{2}{5}$

c)  $3\frac{1}{3} \times 2\frac{2}{5}$

d)  $3\frac{1}{2} \times 4\frac{2}{3}$

e)  $6\frac{2}{5} \times 1\frac{7}{8} \times \frac{7}{12}$



## 5.10 Dividing by Fractions

Dividing by fractions is quite easy. First we **invert** the fraction and then we multiply.

**Example - Find**  $5 \div \frac{1}{3}$

$$5 \div \frac{1}{3} = 5 \times \frac{3}{1} = 5 \times 3 = 15$$

**Example - Find**  $\frac{7}{16} \div \frac{5}{8}$

$$\frac{7}{16} \div \frac{5}{8} = \frac{7}{16} \times \frac{8}{5} = \frac{7}{8 \times 2} \times \frac{8 \times 1}{5} = \frac{7}{2} \times \frac{1}{5} = \frac{7}{10}$$

### Practice

Find

a)  $8 \div \frac{4}{5}$

b)  $18 \div \frac{6}{7}$

c)  $35 \div \frac{5}{7}$

d)  $44 \div \frac{4}{9}$

e)  $36 \div \frac{4}{7}$

f)  $\frac{21}{32} \div \frac{7}{8}$

g)  $\frac{3}{56} \div \frac{9}{14}$

h)  $\frac{21}{22} \div \frac{7}{11}$

i)  $\frac{9}{26} \div \frac{12}{13}$

**Example - Find**  $3\frac{1}{8} \div 8\frac{3}{4}$

**Step 1:** Change mixed numbers to improper fractions.

$$3\frac{1}{8} \div 8\frac{3}{4} = \frac{25}{8} \div \frac{35}{4},$$

**Step 2:** Invert the second fraction.

$$\frac{25}{8} \div \frac{35}{4} = \frac{25}{8} \times \frac{4}{35},$$

**Step 3:** Cancel the common factors

$$\frac{25}{8} \times \frac{4}{35} = \frac{5 \times 5}{4 \times 2} \times \frac{4 \times 1}{5 \times 7} = \frac{5}{2} \times \frac{1}{7},$$

**Step 4:** Find the answer!

$$\frac{5}{2} \times \frac{1}{7} = \frac{5}{14}$$

### Practice

i. Use the steps in the example to find

a)  $5\frac{4}{9} \div \frac{14}{27}$

b)  $4\frac{2}{7} \div \frac{9}{14}$

c)  $3\frac{1}{8} \div 3\frac{3}{4}$

d)  $7\frac{1}{5} \div 1\frac{7}{20}$

ii. Look at the square. Each letter a,b,c,d is a proper fraction in its lowest terms. Use this information to find a,b,c,d:

$$a + b = \frac{3}{4} \quad a \times c = \frac{1}{8}$$

$$d = 3 \times b \quad a \times d = \frac{3}{8}$$

<b>a</b>	<b>b</b>
<b>c</b>	<b>d</b>

**Activity** - What steps are needed to find the answer to this problem?  $2\frac{1}{4} \times \frac{3}{14} \div 1\frac{2}{7}$

Write the steps needed. Compare what you have written with your partner.

When you have the correct steps solve the problem together.

**Step 1:**

**Step 2:**

**Step 3:**

**Step 4:**

# 6. Percentages

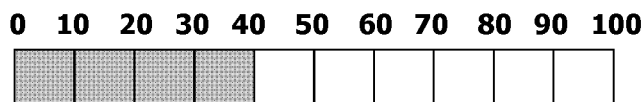
## 6.1 Introduction

Cent is a Latin word for one hundred. **Percent** means per hundred. If 60 per cent of workers in a factory are women then 60 out of every 100 workers are women. We use the symbol % when writing about percentages, 60 per cent = 60 %.

### Think

60 % of workers in a factory are women. There are 200 workers. How many women are there?

## 6.2 Percentages, Fractions and Decimals

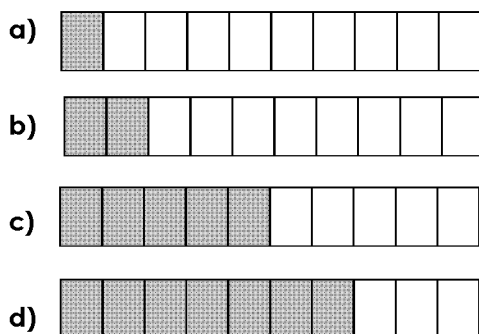


In the diagram 40 parts out of 100 are shaded. As a fraction this is  $\frac{40}{100}$ . As a decimal this is 0.4.

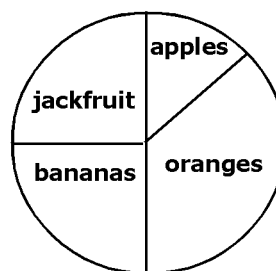
It is also 40 %. We see that  $\frac{40}{100} = 0.4 = 40 \%$ .

### Think

i. Write the shaded part of each diagram as a percentage, a fraction and a decimal.



ii. A class of students was asked which fruit they liked best. The results are in the chart below.



Estimate:

- a) The percentage of students who chose bananas.
- b) The percentage who chose apples.
- c) The percentage that did not choose jackfruit.

We can write fractions and decimals as percentages.

**Example -** Write  $\frac{7}{20}$  as a percentage.

$$\frac{7}{20} = \frac{7}{20} \times 100 \% = 35 \%$$

**Example -** Write 0.7 and 1.24 as percentages.

$$0.7 = 0.7 \times 100 \% = 70 \%$$

$$1.24 = 1.24 \times 100 \% = 124 \%$$

### Think

We can also write percentages as fractions and decimals. Try to write 30 % and 62.5 % as fractions and as decimals.

**Example -** Write  $12\frac{1}{2} \%$  as a fraction.

$$12\frac{1}{2} \% = 12.5 \% = \frac{12.5}{100}$$

$$= \frac{12.5 \times 10}{100 \times 10} = \frac{125}{1000}$$

$$= \frac{1 \times 125}{8 \times 125} = \frac{1}{8}$$

Change to a fraction by dividing by 100.

Multiply the numerator and denominator by 100 to get rid of the decimal point.

Simplify the answer.

## Practice

i. Write as fractions in their lowest terms

- a) 30 %      b) 85 %      c) 42.5 %      d) 5.25 %

ii. Write as decimals

- a) 44 %      b) 68 %      c) 170 %      d)  $16\frac{1}{2}\%$       e)  $28\frac{2}{5}\%$       f)  $235\frac{3}{4}\%$

iii. Complete the table. The first row is completed as an example

	Fraction	Decimal	Hundredths	Percentage
a)	$\frac{1}{10}$	0.1	$\frac{10}{100}$	10 %
b)	$\frac{\quad}{10}$	0.	$\frac{\quad}{100}$	90 %
c)	$\frac{\quad}{10}$	0.8	$\frac{\quad}{100}$	%
d)	$\frac{\quad}{10}$	0.	$\frac{60}{100}$	%
e)	$\frac{3}{10}$	0.	$\frac{\quad}{100}$	%
f)	$\frac{1}{2}$	0.	$\frac{\quad}{100}$	%
g)	$\frac{1}{\quad}$	0.	$\frac{25}{100}$	%
h)	$\frac{3}{4}$	0.	$\frac{\quad}{100}$	%
i)		0.2		

## 6.3 Percentages and Quantities

We can write one **quantity** as a percentage of another. First we divide the first quantity by the second. Then we multiply the fraction by 100 %.

**Example -** Find 4 as a percentage of 20.

$$\frac{4}{20} = \frac{4}{20} \times 100\% = 20\%$$

**Example -** Write 20 cm as a percentage of 3 m.

3 m = 3 x 100 cm = 300 cm. So,

$$\frac{20}{300} \times 100\% = \frac{20}{3}\% = 6\frac{2}{3}\%$$

## Practice

Write the first quantity as a percentage of the second.

- a) 3, 12
- b) 15, 20
- c) 60 cm, 4 m
- d) 600 m, 2 km
- e) 1200 g, 2 kg
- f) 0.01 m, 150 cm
- g) 50 baht, 100 baht
- h) 135 baht, 450 baht

i) In her Maths exam, Thanda scored 28 out of 40. What was her mark as a percentage?

j) Mi Mi earns 800 baht a week working in a factory. She spends 250 baht on food, 100 baht on clothes and saves the remainder. What percentage of her money does she save?

We can also find a percentage of one quantity.

**Example - Find 12 % of 450.**

$$12\% = \frac{12}{100} \text{ So,}$$

$$12\% \text{ of } 450 = \frac{12}{100} \times 450 = 0.12 \times 450 = 54.$$

**Example - Find  $7\frac{1}{3}\%$  of 6 m.**

$$\begin{aligned} 7\frac{1}{3}\% \text{ of } 6 \text{ m} &= 7\frac{1}{3}\% \text{ of } 600 \text{ cm} \\ &= \frac{22}{3}\% \text{ of } 600 \text{ cm} = \frac{22}{3 \times 100} \times 600 \text{ cm} \\ &= \frac{22}{300} \times 600 \text{ cm} = 22 \times 2 \text{ cm} = 44 \text{ cm} \end{aligned}$$

## Practice

Calculate the following:

- a) 40 % of 120
- b) 70 % of 360
- c) 80 % of 1150 g
- d) 63 % of 4 m
- e) 17 % of 2000 m
- f) 12 % of 400 baht
- g)  $5\frac{1}{4}\%$  of 56 mm

h) There are 120 shops in Umphiem camp. 35 % of the shops sell food. How many shops sell food? How many shops do not sell food?

i) It is estimated that 62 % of the refugees in camps on the Thai-Burma border came from Karen state. If there are 150,000 refugees in total, how many came from Karen state?

## 6.4 Percentage Increase and Decrease

If we **increase** a quantity by 30 %, the increased quantity is  $(100 + 30)\% = 130\%$  of the original.

If we **decrease** a quantity by 30 %, the decreased quantity is  $(100 - 30)\% = 70\%$  of the original.

**Example - Increase 180 by 30 %**

The new number is 130 % of the original.

$$130\% \text{ of } 180 = \frac{130}{100} \times 180 = \frac{13}{10} \times 180 = 13 \times 18 = 234$$

The new value is 234.

**Example - Decrease 180 by 30 %**

The new value is 70 % of the original.

$$70\% \text{ of } 180 = \frac{70}{100} \times 180 = \frac{7}{10} \times 180 = 7 \times 18 = 126$$

The new value is 126.

## Practice

i. Increase:

- a) 100 by 40 %
- b) 340 by 60 %
- c) 1600 by 73 %
- d) 145 by 120 %

ii. Decrease

- a) 100 by 30 %
- b) 350 by 40 %
- c) 3400 by 28 %
- d) 250 by  $37\frac{1}{5}\%$

iii. Solve the following:

a) The population of the world is about 6500 million. By 2050 scientists think the population will have increased by about 40 %. What will the world's population be in 2050?

b) The owner of a clothes shop in Mae Sot offers a **discount** on the clothes in her shop. (Discount is money taken away from the price of something).

The table below shows the original price (before the discount) of the clothes and the percentage discount. Complete the table by calculating the new prices.

Type of clothing	Original price	Discount	New price
Jeans	900 baht	35 %	
T-Shirt	250 baht	25 %	
Sandals	175 baht	10 %	
Jacket	1300 baht	50 %	
Shoes	550 baht	20 %	
Shirt	425 baht	15 %	

## 6.5 Finding Percentage Increases and Decreases

**Example** - Naw Cleo bought a motorbike for 40000 baht. She sold it one year later for 34000 baht. What is the percentage decrease in the price?

$$\text{Loss} = 40000 - 34000 = 6000$$

$$6000 = \frac{6000}{40000} \text{ of } 40000.$$

$$\frac{6000}{40000} = \frac{6}{40} = 0.15 = 15 \%$$

First calculate the difference between the two prices.

Then calculate the difference as a fraction of the original price.

Change this fraction to a percentage to get the percentage decrease in price.

### Think

In 1984 there were 10,000 refugees living on the Thai-Burma border. By 1994 the number had increased to 80,000. Can you calculate the percentage increase in the numbers of refugees?

### Practice

i. Find the percentage price increases

a) Buying price 12 baht, selling price 15 baht

b) Buying price 16 baht, selling price 20 baht

c) Buying price 55 baht, selling price 60.50 baht

ii. Find the percentage price decreases

a) Buying price 20 baht, selling price 16 baht

b) Buying price 125 baht, selling price 100 baht

c) Buying price 64 baht, selling price 16 baht

iii. The shop owner in Mae Sot offers a discount on more items in the shop. Find the percentage decrease on the items.

Type of clothing	Original price	Discount	New price
Longyi	200 baht		125 baht
Earrings	50 baht		20 baht
Socks	20 baht		12 baht
Skirt	350 baht		250 baht
Underpants	35 baht		10 baht

## 6.6 Compound Percentage Problems

Sometimes a percentage increase or decrease happens more than once.

**Example -** Htaw Pai bought a motorbike for 35000 baht. The value of the bike decreased by 10 % each year. What is the value of the bike after 3 years?

After 1 year the value of the bike is  $\frac{90}{100} \times 35,000 = 31,500$

After 2 years the value of the bike is  $\frac{90}{100} \times 31,500 = 28,350$

After 3 years the value of the bike is  $\frac{90}{100} \times 28,350 = 25,515$

In the above example we calculated the answer in 3 steps. We also use this formula to calculate the answer in one step:

$$\text{Value after } n \text{ years} = \text{original value} \times \text{multiplier}^n$$

In this example multiplier =  $\frac{90}{100} = 0.9$

### Practice

i. Use the formula to find the value of Htaw Bai's motorbike after 5 years. (Use the fact that  $0.9^5 = 0.59$  to 2 decimal places).

The following two problems deal with compound percentage *increases*

ii. The population of Israel is 7,000,000 to the nearest million. This figure is increasing by around 2 % each year. What will be the population of Israel in 20 years? (Use the fact that  $1.02^{20} = 1.5$  to 1 decimal place).

iii. China uses 6.6 million barrels of oil everyday. The amount the country uses has increased by an average of 7 % per year since 1990. If this growth continues how many barrels of oil will China use per day in 5 years? (Use the fact that  $1.07^5 = 1.4$  to 1 decimal place).

# 7. Ratio

## 7.1 Introduction

We use **ratios** to compare **related** quantities.

**Example** - Nang Hseng and Sai Lek have 18 grandchildren: 10 grandsons and 8 granddaughters. The ratio of the number of grandsons to the total number of grandchildren is 10 to 18.

We can write this as a fraction:  $\frac{\text{Number of grandsons}}{\text{Total number of grandchildren}} = \frac{10}{18} = \frac{5}{9}$

or as a ratio: Number of grandsons : total number of grandchildren = 10 : 18 = 5 : 9.

We simplify ratios in the same way as we simplify fractions.

### Think

- a) What is the ratio of the number of granddaughters to the number of grandchildren?  
Simplify your answer.
- b) What is the ratio of the number of granddaughters to the number of grandsons?

## 7.2 Simplifying Ratios

**Example** - Simplify the ratio 2 cm to 1 m.

Before we compare, the quantities must have the same units.

$$2 \text{ cm} : 1 \text{ m} = 2 \text{ cm} : 100 \text{ cm} = 1 : 50$$

We do not need to write the units but we say, 'the ratio of 2 cm to 1 m is 1 to 50'.

**Example** - Simplify the ratio  $2 : \frac{1}{3}$

Here we use multiplication:

$$2 : \frac{1}{3} = 2 \times 3 : \frac{1}{3} \times 3 = 6 : 1$$

**Example** - Simplify the ratio 24 to 72.

$$\begin{aligned} 24 : 72 &= 3 \times 8 : 9 \times 8 = 3 : 9 \\ &= 1 \times 3 : 3 \times 3 = 1 : 3 \end{aligned}$$

**Example** - Simplify the ratio  $\frac{2}{3} : \frac{1}{5}$

We need to multiply by the lowest common multiple to make whole numbers

$$\begin{aligned} \frac{2}{3} : \frac{1}{5} &= 15 \times \frac{2}{3} : 15 \times \frac{1}{5} \\ &= 5 \times 2 : 3 \times 1 = 10 : 3 = 10 : 3 \end{aligned}$$

### Practice

i. Simplify the ratios:

a) 8 : 10

b) 12 : 18

c) 32 baht : 96 baht

d) 12 cm to 2 m

e) 4 : 6 : 10

f) 144 : 12 : 24

g) 7 : 56 : 49

h)  $5 : \frac{1}{3}$

i)  $\frac{1}{3} : \frac{3}{4}$

j)  $\frac{5}{4} : \frac{6}{7}$

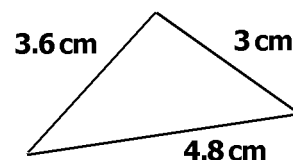
k)  $\frac{1}{6} : \frac{1}{8} : \frac{1}{12}$

ii. Solve the following:

a) Moe Aye walks 2 km to school in 40 minutes. Nai Aung cycles 5 km to school in 15 minutes. What is the ratio of i) Moe Aye's distance to Nai Aung's distance and ii) Moe Aye's time to Nai Aung's time.

b) Earlier we learnt that Naw Kaw's harvest was  $5\frac{1}{2}$  kg of corn,  $2\frac{1}{4}$  kg of green beans and 7 kg of cucumber. Find the ratio of the amount of vegetables to one another.

c) Find the ratio of the sides of the triangle to one another.



## 7.3 Finding Quantities

**Example -** Find the missing number:  $\_ : 4 = 3 : 5$

Fill the gap with an  $X$ ,  $X : 4 = 3 : 5$ .

Write as fractions,  $\frac{X}{4} = \frac{3}{5}$

Multiply by 4,  $4 \times \frac{X}{4} = 4 \times \frac{3}{5}$

This gives  $X = \frac{12}{5} = 2\frac{2}{5}$

So,  $2\frac{2}{5} : 4 = 3 : 5$

**Example -** Two distances are in the ratio  $12 : 5$ .

The first distance is 8 km. Find the second distance.

Let  $X$  be the second distance,  $8 : X = 12 : 5$ .

So,  $\frac{X}{8} = \frac{5}{12}$ .

Multiply by 8,  $8 \times \frac{X}{8} = 8 \times \frac{5}{12}$

This gives  $X = \frac{10}{3} = 3\frac{1}{3}$

So the second distance is  $3\frac{1}{3}$  km

### Practice

i. Find the missing numbers:

- a)  $2 : 5 = 4 : \_$       b)  $\_ : 6 = 12 : 18$       c)  $9 : 6 = \_ : 4$       d)  $\_ : 9 = 3 : 5$   
 e)  $9 : 5 = \_ : 4$       f)  $\_ : 3 = 5 : 2$       g)  $3 : \_ = 5 : 1$       h)  $\_ : 6 = 5 : 8$

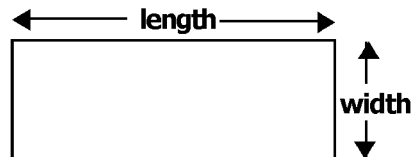
ii. Find the second quantity:

a) Two distances are in the ratio  $12 : 8$ . The first distance is 8 km. Find the second distance.

b) If the ratio in question a) was  $8 : 12$ , what would the second distance be?

c) The ratio of Shine's money to Htoo Chit's money is  $8 : 10$ . Htoo Chit has 25 baht. How much money does Shine have?

d) In the rectangle, the ratio of length to width is  $9 : 4$ . The length is 24 cm. What is the width?



## 7.4 Sharing Quantities

**Example -** Share 60 baht between Hser Moo and Hsa Say in the ratio  $3 : 2$ .

number of shares needed:	$3 + 2 = 5$
value of 1 share:	$60 \div 5 = 12$
value of 2 shares:	$2 \times 12 = 24$
value of 3 shares:	$3 \times 12 = 36$

Hser Moo gets 3 shares, which is 36 baht. Hsa Say gets 2 shares, which is 24 baht.

### Think

Look at the amounts that Hser Moo and Hsa Say received. How do we know if the answer is right? How much would they get if the ratio was  $2 : 4$ ?

### Practice

- a) Share 80 baht in the ratio  $3 : 2$   
 b) Share 32 baht in the ratio  $3 : 5$   
 c) Share 45 baht in the ratio  $4 : 5$   
 d) Divide 26 baht in the ratio  $4 : 5 : 4$

## 7.5 Map Scales

We use map scales to measure real distances between places. Look at the map on the next page.

The scale is  $1 : 100\,000$ . This means 1 cm on the map is 100 000 cm in real distances.

$100\,000\text{ cm} = 1000\text{ m} = 1\text{ km}$ , so 1 cm on the map is 1 km in real distances.

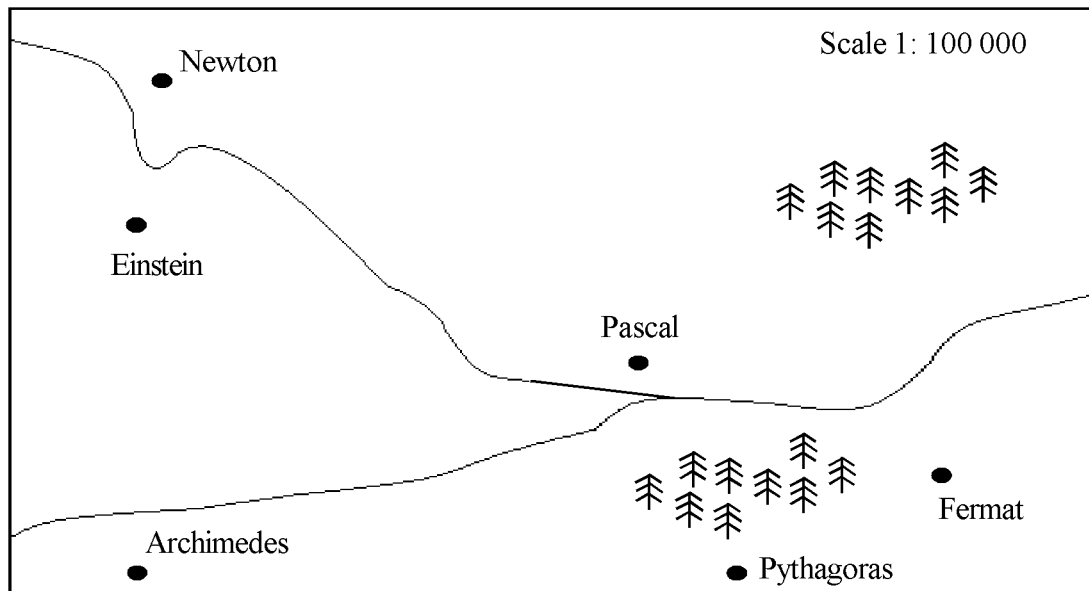


**Activity** - The map is of a country named Geekland. Each town is named after a famous mathematician. The distance between Archimedes and Pythagoras on the map is 8 cm. How far is it from Archimedes to Pythagoras in kilometres?

Use a ruler to measure the distance on the map between:

- a) Pythagoras and Newton
- b) Pascal and Einstein
- c) Pascal and Fermat
- d) Archimedes and Newton

Now find the real distances using the map scale.



## 8. Indices

### 8.1 Positive Indices

In Section 2.3 we learnt about numbers with positive indices.

We learnt how to write in index form:

$$3 \times 3 \times 3 \times 3 = 3^4$$

And how to find the value of numbers in index form:

$$2^5 = 2 \times 2 \times 2 \times 2 \times 2 = 32$$

**We can multiply different powers of the same number by adding the indices:**

$$2^2 \times 2^3 = 2^{2+3} = 2^5$$

### Think

a) Complete the statement to write  $2^5 \div 2^3$  as a single number in index form:

$$2^5 \div 2^3 = 2^{\underline{\quad}} = \underline{\quad} =$$

b) Fill in the missing word and complete the statement:

We can divide different powers of the same number by                      the indices:

$$2^5 \div 2^3 = 2^{\quad} =$$

### Practice

Write as a single number in index form:

a)  $3^5 \times 3^2$

b)  $7^5 \times 7^3$

c)  $5^4 \times 5^4$

d)  $12^4 \times 12^5$

e)  $4^4 \div 4^2$

f)  $10^8 \div 10^3$

g)  $2^3 \div 2^3$

h)  $6^{12} \div 6^7$

i)  $15^8 \div 15^4$

j)  $2^2 \times 2^4 \times 2^3$

k)  $4^2 \times 4^3 \div 4^4$

l)  $3^6 \div 3^2 \times 3^4$

Look at question g). The answer is  $2^3 \div 2^3 = 2^0$ .

$$\text{Also, } 2^3 \div 2^3 = \frac{2 \times 2 \times 2}{2 \times 2 \times 2} = 1.$$

**Any number with an index of zero is equal to one:**

$$2^3 \div 2^3 = 2^0 = 1.$$

## 8.2 Negative Indices

**Example** - Find the value of  $2^3 \div 2^5$

Subtracting the indices gives:

$$2^3 \div 2^5 = 2^{3-5} = 2^{-2}$$

As a fraction we have:

$$2^3 \div 2^5 = \frac{2^3}{2^5} = \frac{2 \times 2 \times 2}{2 \times 2 \times 2 \times 2 \times 2} = \frac{1}{2^2}$$

$$\text{The value of } 2^3 \div 2^5 = 2^{-2} = \frac{1}{2^2} = \frac{1}{4}$$

$\frac{1}{2^2}$  is called the **reciprocal** of  $2^2$ .  
Also,  $2^2$  is called the reciprocal of  $\frac{1}{2^2}$ .

### Practice

i. Find the reciprocal of:

- a)  $2^4$                       c)  $7^{-3}$   
b)  $7^3$                       d)  $5^{-5}$

ii. Write as a single number in index form:

- a)  $5^2 \div 5^4$                       c)  $10^3 \div 10^6$   
b)  $6^4 \div 6^7$                       d)  $a^5 \div a^7$

iii. Find the value of:

- a)  $2^{-3}$                       d)  $8^{-2}$   
b)  $3^{-3}$                       e)  $5^3 \div 5^6$   
c)  $7^{-2}$                       f)  $4^{-1} \times 4^{-2}$

## 8.3 Standard Form

In Section 4.6, you were asked to guess the distance to the moon. The answer is 400,000 km. When measuring large numbers like this, scientists use **standard form**:

$$400,000 = 4 \times 10 \times 10 \times 10 \times 10 \times 10 = 4 \times 10^5$$

Standard form is a number between 1 and 10 multiplied by a power of 10.

**Example** - Write 68,000 in standard form.

$$68\,000 = 6.8 \times 10,000 = 6.8 \times 10^4$$

**Example** - Write 0.01934 in standard form.

$$0.01934 = 1.934 \div 100 = 1.934 \times \frac{1}{100} = 1.934 \times 10^{-2}$$

### Practice

i. Write the following in standard form:

- a) 2500                      g) 0.79  
b) 630                      h) 0.0048  
c) 39,070                      i) 0.0805  
d) 260,000                      j) 0.08808  
e) 4,060,000                      k) 0.684  
f) 80,000,000,000                      l) 0.000 000 000 073

ii. Write the following as ordinary numbers:

- a)  $3.78 \times 10^3$                       d)  $3.76 \times 10^{-6}$   
b)  $1.26 \times 10^{-3}$                       e)  $4.25 \times 10^{12}$   
c)  $5.3 \times 10^6$                       f)  $4.43 \times 10^{-8}$

## 8.4 Significant Figures

### Think

Ti Reh is 1678 mm tall. How tall is he:

- a) to the nearest 10 mm?  
b) to the nearest cm?  
c) in metres (to 2 d.p.)?  
d) in km (to 5 d.p.)?

The numbers 1, 6 and 8 appear in each answer. 1, 6 and 8 are called the **significant figures (s.f.)**. Each answer is given to 3 significant figures. The first significant figure is 1. The second is 6. The third is 8.

In standard form the first significant figure is the number in the tens column.

**Example** - Find:

- a) the 1st significant figure and  
b) the 3rd significant figure  
of 0.001503.

$$\text{In standard form } 0.001503 = 1.503 \times 10^{-3}.$$

- a) The first significant figure is 1.  
b) The third significant figure is 0.

### Practice

Write down the significant figure given in brackets.

- a) 36.2 (1st)                      d) 34.807 (4th)  
b) 0.0867 (2nd)                      e) 0.07603 (3rd)  
c) 3.786 (3rd)

**Example** - Give 32685 correct to 1 s.f.

$$32685 = 3.2685 \times 10^4.$$

3 is the first s.f. The 2nd s.f. is less than 5, so we round down.

$$\text{So, } 32685 = 3 \times 10^4 = 30000 \text{ to 1 s.f.}$$

**Example** - Give 0.02186 correct to 3 s.f.

$$0.02186 = 2.186 \times 10^{-2}.$$

Here the 4th s.f. is greater than 5 so we round up.

$$\text{So, } 0.02186 = 2.19 \times 10^{-2} = 0.0219 \text{ to 3 s.f.}$$

### Practice

i. Give the following numbers correct to 1 s.f.

a) 59727

d) 26

b) 476

e) 4099

c) 586359

f) 4396359

ii. Give the following numbers correct to 2 s.f.

a) 4674

d) 72601

b) 58700

e) 444

c) 9973

f) 53908

iii. Give the following numbers correct to 3 s.f.

a) 0.008463

d) 7.5078

b) 5.8374

e) 369.649

c) 46.8451

f) 0.0078547

## 8.6 Square Roots

We know that  $3^2 = 9$ . 3 is the square root of 9. In section 3.4 we learnt that  $(-3)^2 = 9$ . -3 is also the square root of 9. In this module we will study positive square roots.

The square root symbol is  $\sqrt{\quad}$ . We write  $\sqrt{9} = 3$ .

**Example** - Find the square root of 0.49.

$$0.49 = 0.7^2. \text{ So, } \sqrt{0.49} = 0.7$$

### Practice

Find the square roots:

a)  $\sqrt{9}$

b)  $\sqrt{25}$

c)  $\sqrt{64}$

d)  $\sqrt{1}$

e)  $\sqrt{4900}$

f)  $\sqrt{0.64}$

g)  $\sqrt{0.04}$

In section 2.4 we learnt about prime factors. Prime factors can help us find square roots.

**Example** - Find the square root of 784.

As a product of prime factors  $784 = 2^2 \times 2^2 \times 7^2$ .

We can write  $2^2 \times 2^2 \times 7^2 = (2 \times 2 \times 7)^2 = 28^2$ .

$$\text{So, } 784 = 28^2 \text{ and } \sqrt{784} = \sqrt{28^2} = 28$$

### Practice

Find the square roots:

a)  $\sqrt{576}$

b)  $\sqrt{1296}$

c)  $\sqrt{1764}$

The numbers above have whole number square roots. Most numbers do not. If we do not have a calculator, we have to estimate the square root.

**Example** - Find the square root of 23.

We know that  $16 < 23 < 25$ . If we take the square roots we have:  $\sqrt{16} < \sqrt{23} < \sqrt{25} = 4 < \sqrt{23} < 5$

We learn that  $\sqrt{23}$  is between 4 and 5. So, to 1 significant figure  $\sqrt{23} = 4$ .

### Practice

Find the first significant figure of the square roots of these numbers:

a) 17

b) 10

c) 39

d) 79

e) 90

## 8.7 Surds

The area of the square is 20 cm. The length of the side is  $x$  cm. So,

$$x^2 = 20$$

$$x = \sqrt{20}$$

If we use a calculator we would find that  $x = 4.47$  to 2 decimal places. To represent the number exactly we can just write  $x = \sqrt{20}$ . A number written exactly in this form is called a **surd**. Other examples of numbers in surd form are:  $\sqrt{3}$ ,  $2 - \sqrt{5}$ ,  $\frac{\sqrt{2}}{2}$

**Example - Simplify**  $\sqrt{12}$

$$\sqrt{12} = \sqrt{4 \times 3} = \sqrt{4} \times \sqrt{3} = 2\sqrt{3}$$

**Example - Rationalise\***  $\frac{1}{3\sqrt{5}}$

We need to multiply the top and bottom by  $\sqrt{5}$

$$\frac{1}{3\sqrt{5}} = \frac{1}{3\sqrt{5}} \times \frac{\sqrt{5}}{\sqrt{5}} = \frac{\sqrt{5}}{3 \times 5} = \frac{\sqrt{5}}{15}$$

**Example - Rationalise\***  $\frac{\sqrt{2}}{5 + \sqrt{2}}$

Multiply the top and bottom by  $(5 - \sqrt{2})$

$$\frac{\sqrt{2}}{5 + \sqrt{2}} = \frac{\sqrt{2}(5 - \sqrt{2})}{(5 + \sqrt{2})(5 - \sqrt{2})}$$

$$= \frac{5\sqrt{2} - 2}{25 - 5\sqrt{2} + 5\sqrt{2} - 2} = \frac{5\sqrt{2} - 2}{23}$$

\* **Rationalise** means to remove the square root in the denominator

### Practice

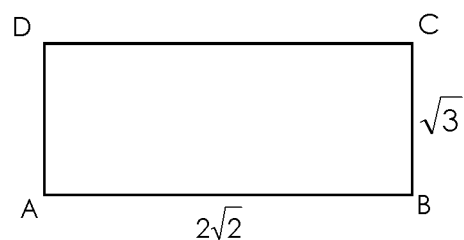
i. a)  $\frac{1}{\sqrt{7}}$     b)  $\frac{1}{\sqrt{17}}$     c)  $\frac{\sqrt{32}}{\sqrt{2}}$     d)  $\frac{\sqrt{5}}{3 + \sqrt{5}}$     e)  $\frac{\sqrt{7}}{2 - \sqrt{7}}$     f)  $\frac{\sqrt{3}}{2 - \sqrt{3}}$

ii. The lengths of the sides of a rectangle are  $3 + \sqrt{5}$  and  $3 - \sqrt{5}$ . Find:

a) The perimeter of the rectangle      b) The area of the rectangle

iii. The rectangle shown has sides  $2\sqrt{2}$  and  $\sqrt{3}$ .

Find the length of the diagonal (using Pythagoras' theorem)



# 9. Estimation

## 9.1 Using Significant Figures to Estimate

At the beginning of this module, we learnt how to use rounding to estimate answers. We can also use significant figures to give estimates.

**Example** - Correct each number to 1 s.f. and give an estimate:

a)  $9.524 \times 0.0837$

$$9.524 \times 0.0837 \approx 10 \times 0.08 = 8$$

This symbol means 'approximately equal to'.

b) 
$$\frac{0.048 \times 3.275}{0.367}$$

$$\frac{0.048 \times 3.275}{0.367} \approx \frac{0.05 \times 3}{0.4} = \frac{0.15}{0.4} = \frac{1.5}{4} = 0.4$$

The answer is given to 1 s.f.

### Practice

Correct each number to 1 s.f. and give an estimate:

a)  $4.78 \times 23.7$

b)  $0.0674 \times 5.24$

c) 
$$\frac{3.87 \times 5.24}{2.13}$$

d) 
$$\frac{0.636 \times 2.63}{5.57}$$

**Activity** - Look at the exercise below and match the calculation with the estimate by correcting each number to 1 significant figure. When you have finished make your own exercise by writing some calculations and corresponding estimates. Give your exercise to your partner to solve.

$$\frac{4.257}{83.6}$$

$$0.827 \div 0.093$$

$$64$$

$$\frac{80}{9}$$

$$(3.827)^3$$

$$\frac{2.27 \times 3.84}{5.01}$$

$$\frac{1}{10}$$

$$0.532 \times 3.621 \times 36$$

$$2.6$$

$$72$$

$$\frac{2.93 \times 0.0372}{1.84 \times 0.562}$$

$$\frac{1}{20}$$

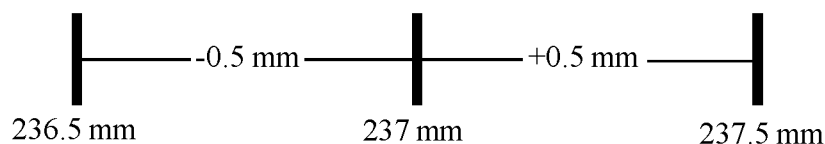
## 9.2 Upper and Lower Bounds

Consider the measurement:

237 mm, correct to the nearest millimetre

'correct to the nearest millimetre' means that the measurement has been rounded up or down.

The actual length could be anywhere between 236.5 mm and 237.5 mm.



236.5 is the smallest possible value - it is the **lower bound**.

237.5 is the largest possible value - it is the **upper bound**.

**Example** - Write the lower bound and upper bound for 4.7, correct to 1 decimal place.

The lower bound is 4.65

The upper bound is 4.75

### Practice

Write the upper and lower bound for each measurement

i.

a) To the nearest 10: 30, 180, 3020, 10

b) To 1 decimal place: 2.9, 13.6, 0.3, 157.5

ii. Complete the table attendances at football stadiums

Stadium	Attendance to the nearest thousand	Lower bound	Upper bound
Manchester United	71,000		
Arsenal	42,000		
West Ham	23,000		
Liverpool	13,000		
Morecambe	1,000		

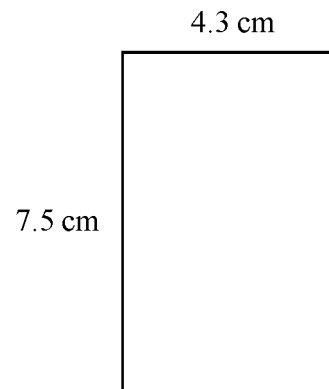
**Example -** A rectangle has width 4.3 cm and length 7.5 cm, correct to the nearest 0.1 cm. Find:

- a) The lower bounds of the length and width
- b) The upper bounds of the length and width
- c) The maximum possible area

a) The lower bound for the length is 7.45 cm  
The lower bound for the width is 4.25 cm

b) The upper bound for the length is 7.55 cm  
The upper bound for the width is 4.35 cm

c) The maximum possible area is  $7.55 \text{ cm} \times 4.35 \text{ cm} = 32.8425 \text{ cm}^2$   
(Using the upper bounds)



### Practice

i. Two circles have radius  $r = 1.7$ , correct to 1 decimal place and  $R = 31$ , correct to 3 significant figures.

- a) Write down the upper and lower bounds of  $r$  and  $R$ .
- b) Find the smallest possible value of  $R - r$ .

ii. The length of each side of a square is 3.7 cm, correct to 2 significant figures.

- a) Find the maximum value for the perimeter of the square
- b) Find the minimum value for the perimeter of the square

iii. Find the upper bound and lower bound of:

- a) The area of a rectangle with sides 6 cm and 8 cm, both correct to the nearest centimetre
- b) The perimeter of a square with side 7.5 cm, correct to the nearest centimetre
- c) The area of a triangle with base 8 cm and height 6 cm, correct to the nearest centimetre

# Glossary of Keywords

Here is a list of Mathematical words from this module. The section where the word appears is given in brackets. Find the words and what they mean - your teacher will test your memory soon!

Whole number	(1.1)	Metre (m)	(4.4)
Value	(1.2)	Kilometre (km)	(4.4)
Order	(1.2)	Centimetre (cm)	(4.4)
Rounding	(1.3)	Millimetre (mm)	(4.4)
Estimate	(1.3)	Mass	(4.5)
Round up/Round down	(1.3)	Tonne (t)	(4.5)
Property	(1.4)	Gram (g)	(4.5)
Addition	(1.4)	Kilogram (kg)	(4.5)
Subtraction	(1.4)	Pentagon	(4.8)
Commutative Law	(1.4)	Decimal Places (d.p.)	(4.9)
Multiplication	(1.5)		
Division	(1.5)	Numerator	(5.1)
Remainder	(1.5)	Denominator	(5.1)
Operation	(1.6)	Proper Fraction	(5.1)
Brackets	(1.6)	Improper Fraction	(5.2)
Powers	(1.6)	Mixed Numbers	(5.2)
Order of operations	(1.6)	Equivalent Fractions	(5.3)
		Multiplication Wall	(5.3)
Factor	(2.1)	Simplify	(5.4)
Product	(2.1)	Common Factors	(5.4)
Multiple	(2.1)	Cancelling	(5.4)
Prime Number	(2.2)	Lowest Terms	(5.4)
Index	(2.3)	Fraction Wall	(5.5)
Indices	(2.3)	Common Denominator	(5.5)
Prime Factor	(2.4)	Recurring Decimal	(5.6)
Highest Common Factor (H.C.F.)	(2.5)	Recur	(5.6)
Lowest Common Multiple (L.C.M.)	(2.6)	Invert	(5.10)
Positive number	(3.1)	Percent	(6.1)
Negative number	(3.1)	Percentages	(6.1)
Temperature	(3.2)	Quantity	(6.3)
Degrees Celsius/Centigrade	(3.2)	Increase	(6.4)
Expand	(3.4)	Decrease	(6.4)
		Discount	(6.4)
Decimal Point	(4.1)		
Tenths	(4.1)	Ratio	(7.1)
Hundredths	(4.1)	Related Quantities	(7.1)
Thousandths	(4.1)		
Perimeter	(4.2)	Reciprocal	(8.2)
Rectangle	(4.2)	Standard Form	(8.3)
Metric Units	(4.4)	Significant Figures	(8.4)
Length	(4.4)	Approximately	(8.5)
		Surd	(8.7)
		Rationalise	(8.7)
		Lower Bound	(9.2)
		Upper Bound	(9.2)

# Assessment

This assessment is written to test your understanding of the module. Review the work you have done before taking the test. Good luck!

## Part 1 - Vocabulary

These questions test your knowledge of the keywords from this module. Complete the gaps in each sentence by using the words in the box. Be careful, there are 20 words but only 15 questions!

commutative		equivalent	property	factor	approximately	kilometres
reciprocal	perimeter	length	estimate	rationalise	numerator	recurring
metres	brackets	multiple	operations	denominator	simplify	standard form

- a)  $2^{-2}$  is the \_\_\_\_\_ of  $2^2$ .
- b) We \_\_\_\_\_ to remove the square root in the denominator
- c) The distance between London and Manchester is measured in \_\_\_\_\_.
- d) When calculating we expand the \_\_\_\_\_ before multiplying.
- e) Multiplication and division are \_\_\_\_\_.
- f) 2 is a \_\_\_\_\_ of 18.
- g) 18 is a \_\_\_\_\_ of 2.
- h) The \_\_\_\_\_ is the distance all the way around.
- i) The \_\_\_\_\_ is the bottom number in a fraction.
- j) \_\_\_\_\_ fractions have the same value.
- k) If we \_\_\_\_\_  $\frac{9}{24}$  the answer is  $\frac{3}{8}$ .
- l) 0.666666666666.... is a \_\_\_\_\_ decimal.
- m) Scientists use \_\_\_\_\_ to write large numbers.
- n) A proper fraction has a \_\_\_\_\_ that is less than the denominator.
- o)  $\approx$  means \_\_\_\_\_ equal to.

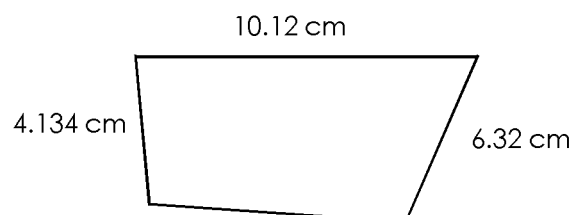


## Part 2 - Mathematics

These questions test your understanding of the Mathematics in this module. Try to answer all the questions. Write your calculations and answers on separate paper.

1. Write these numbers as words: **a)** 201                      **b)** 1021                      **c)** 112354
2. Write these as numbers:  
**a)** seven thousand six hundred and two                      **b)** thirty two thousand and fifty seven  
**c)** one hundred and eleven thousand
3. Solve:  
**a)**  $3021 + 926$                       **b)**  $9217 + 3216 + 824$                       **c)**  $526 - 316$                       **d)**  $1237 - 524$   
**e)** Subtract five thousand one hundred and forty seven from nine thousand three hundred and forty two.
4. Solve:  
**a)**  $798 \times 583$                       **b)**  $7281 \times 694$                       **c)**  $2050 \div 19$                       **d)**  $7974 \div 17$
5. Solve:  
**a)**  $7 + 3 \times 2 - 8 \div 2$                       **b)**  $19 + 3 \times 2 - 4 \div 2$                       **c)**  $6 \times 8 - 18 \div (2 + 4)$                       **d)**  $5 + (2 \times 10 - 5) - 6$
6. **a)** Write down all the multiples of 5 between 19 and 49.  
**b)** Write down all the multiples of 11 between 50 and 100.
7. Which of these numbers are prime numbers:  
41, 57, 82, 91, 101, 126, 135
8. Use a factor tree to write each number as a product of prime factors:  
**a)** 24                      **b)** 136                      **c)** 528
9. Find the Highest Common Factor of:  
**a)** 8, 16                      **b)** 36, 48                      **c)** 18, 20, 36
10. Find the Lowest Common Multiple of:  
**a)** 6, 16                      **b)** 36, 16                      **c)** 85, 50
11. Solve:  
**a)**  $5 + (-1) - (-3)$                       **b)**  $8 - (-7) + 2$                       **c)**  $5 - (6 - 10)$                       **d)** Subtract 7 from -5
12. Complete the statements:  
**a)** A negative number divided by a negative number gives a \_\_\_\_\_ answer.  
**b)** A positive number multiplied by a \_\_\_\_\_ number gives a negative answer.  
**c)** A \_\_\_\_\_ number multiplied by a negative number gives a \_\_\_\_\_ answer.
13. Copy and complete the table so that each row, column and diagonal is equal to 18.9.
14. The perimeter of the shape is 27 cm. What is the length of the fourth side?

		<b>8.1</b>
<b>5.4</b>	<b>6.3</b>	<b>7.2</b>
	<b>10.8</b>	



15. Find the following. Write your answer in the units given in brackets:  
**a)**  $8 \text{ m} - 52 \text{ cm}$  (cm)                      **b)**  $20 \text{ g} - 120 \text{ mg}$  (mg)                      **c)**  $3.9 \text{ m} + 582 \text{ mm}$  (cm)

16. Solve:

a)  $2.16 \times 0.082$

b)  $0.081 \times 0.32$

c)  $8.2 \times 2.8$

d)  $9.8 \div 1.4$

e)  $10.24 \div 3.2$

17. 50 students were asked 'What is your favourite sport?'. The results are in the table.

football	caneball	volleyball	total
15	25	10	50

What fraction chose (write the answer in its lowest terms):

a) football?

b) caneball?

c) volleyball?

18. Write these as mixed numbers:

a)  $\frac{41}{8}$

b)  $\frac{67}{5}$

19. Write these as improper fractions:

a)  $2\frac{6}{7}$

b)  $4\frac{7}{9}$

20. Solve the following:

a)  $\frac{1}{4} + \frac{7}{10}$

b)  $\frac{5}{8} - \frac{2}{7}$

c)  $\frac{4}{5} \times \frac{15}{16}$

d)  $\frac{28}{27} \div \frac{4}{9}$

21. Write these percentages as fractions in their lowest terms:

a) 45 %

b) 56.5 %

c) 9.25 %

22. Calculate the following:

a) 20 % of 200 baht

b) 37 % of 9 m

23. Increase:

a) 150 by 50 %

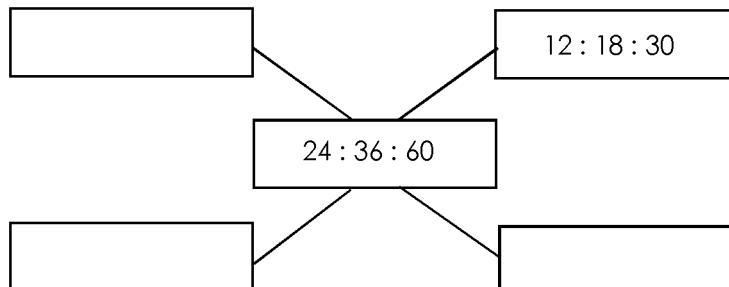
b) 350 by 20%

24. Decrease:

a) 350 by 40 %

b) 750 by 13 %

25. Write ratios equivalent to the one in the centre. What is the simplest form of this ratio?



26. Two lengths are in the ratio 3 : 7. The second length is 42 cm. What is the first length?

27. Write as a single number in index form:

a)  $5^5 \times 5^5$

b)  $7^7 \div 7^3$

c)  $6^3 \div 6^3$

28. Write the following in standard form:

a) 25,000

b) 765

c) 9,000,000,000

29. Write the following to: 3 significant figures:

a) 0.006758

b) 22.8762

c) 542.482

30. Rationalise

a)  $\frac{3}{\sqrt{5}}$

b)  $\frac{1}{\sqrt{11}}$

c)  $\frac{\sqrt{11}}{\sqrt{11} - 7}$

31. Write the upper and lower bounds for each measurement

To the nearest 0.5 unit: 4.5, 7.5, 16.5